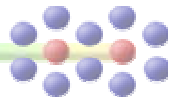


COUPLED-CAVITY STRUCTURES IN PHOTONIC CRYSTALS

**MEHMET BAYINDIR
EKMEL OZBAY**

Department of Physics, Bilkent University, Turkey



➤ Motivations

➤ Underlying Physics

- Investigation of coupled-cavity structures: FDTD, TMM, experiment, and tight-binding approximation

 - Localized cavity modes

 - Eigenmode splitting

 - Photonic molecules

- Observation of a new type of waveguiding mechanism: Coupled-cavity waveguides (CCWs)

➤ Possible Applications

- Waveguides, waveguide bends, splitters, switches

- WDM: adding or dropping a selective wavelength or band

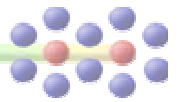
- Strong enhancement of the spontaneous emission

- Increasing efficiency of nonlinear processes

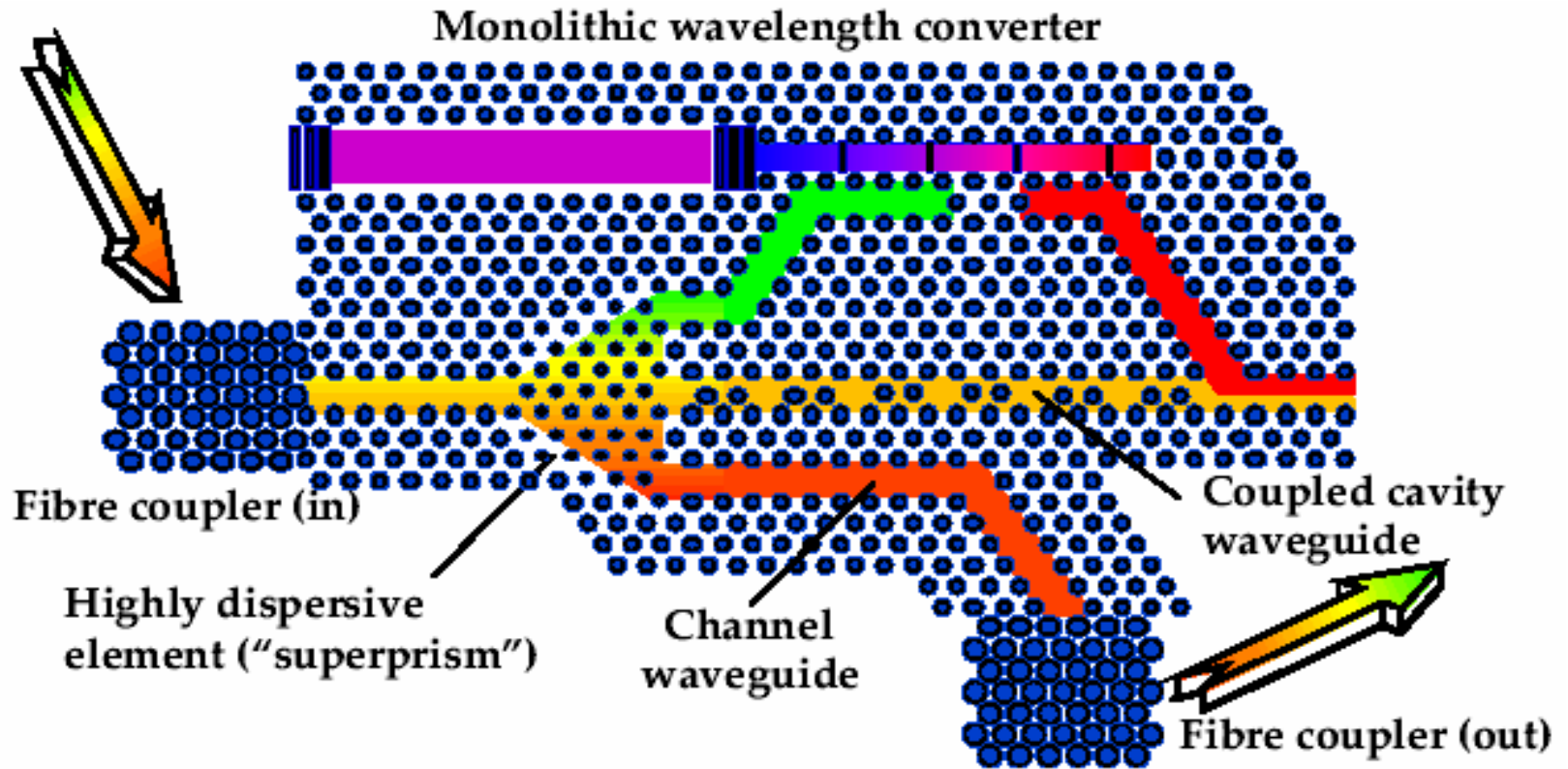
- Dispersion compensators

➤ Summary

MOTIVATIONS



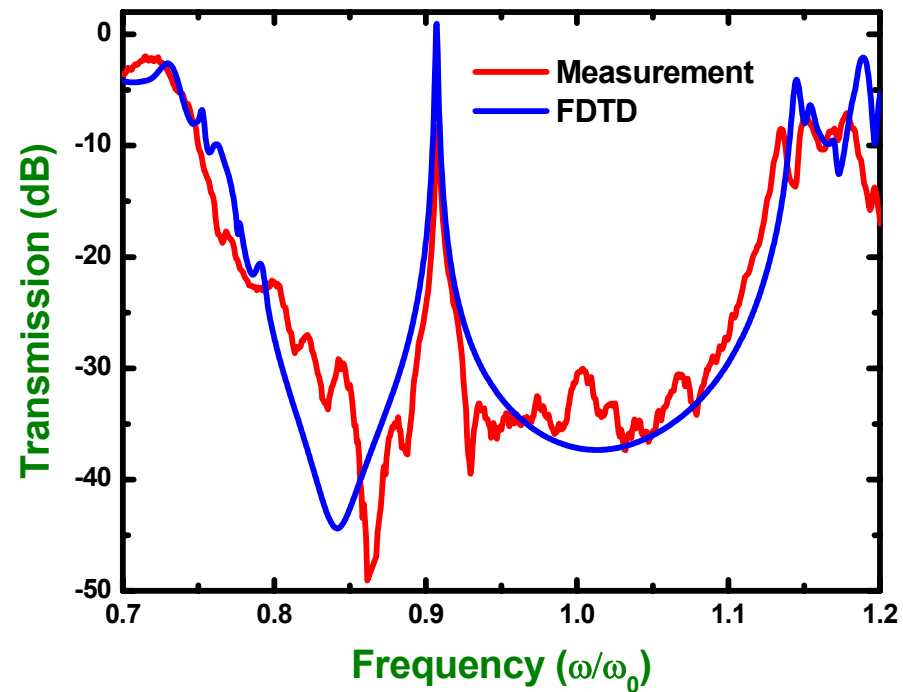
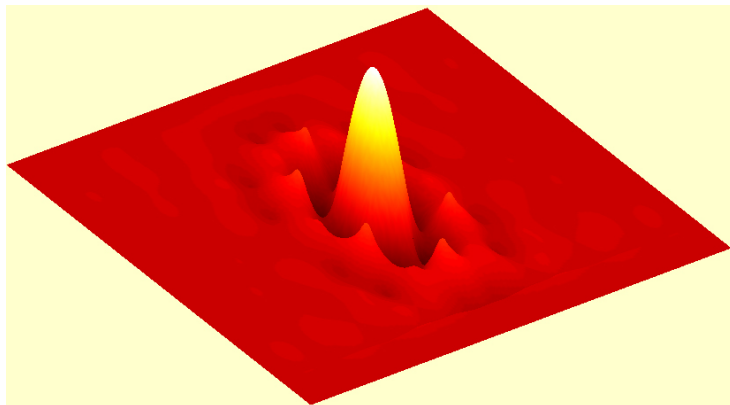
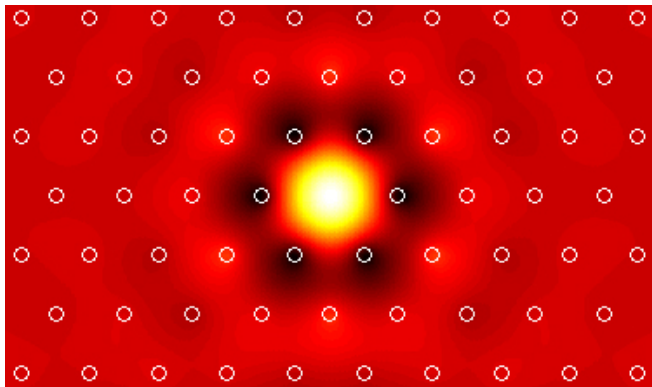
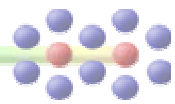
PHOTONIC INTEGRATED CIRCUIT



[from Krauss' paper]

TO CONSTRUCT ALL OPTICAL COMPONENTS ON A SINGLE CHIP

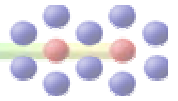
2D PHOTONIC CRYSTALS: LOCALIZED CAVITY MODE



$$\nabla \times [\nabla \times \mathbf{E}_\Omega(\mathbf{r})] = (\Omega_0/c)^2 \varepsilon_0(\mathbf{r}) \mathbf{E}_\Omega(\mathbf{r})$$

**Observation of strongly localized cavity modes within the photonic band gap
analogous to acceptor impurity state in semiconductors**

EIGENMODE SPLITTING

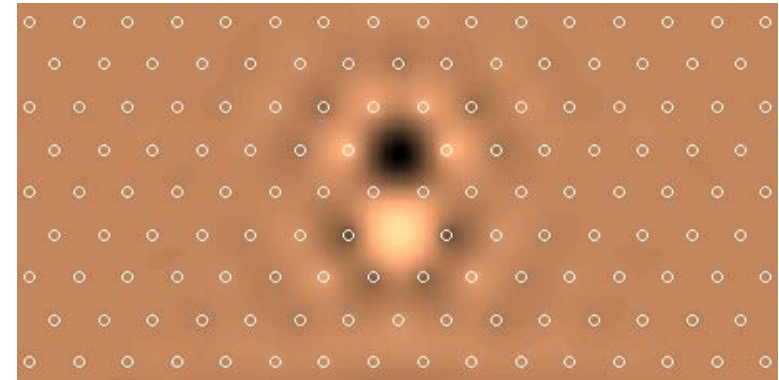
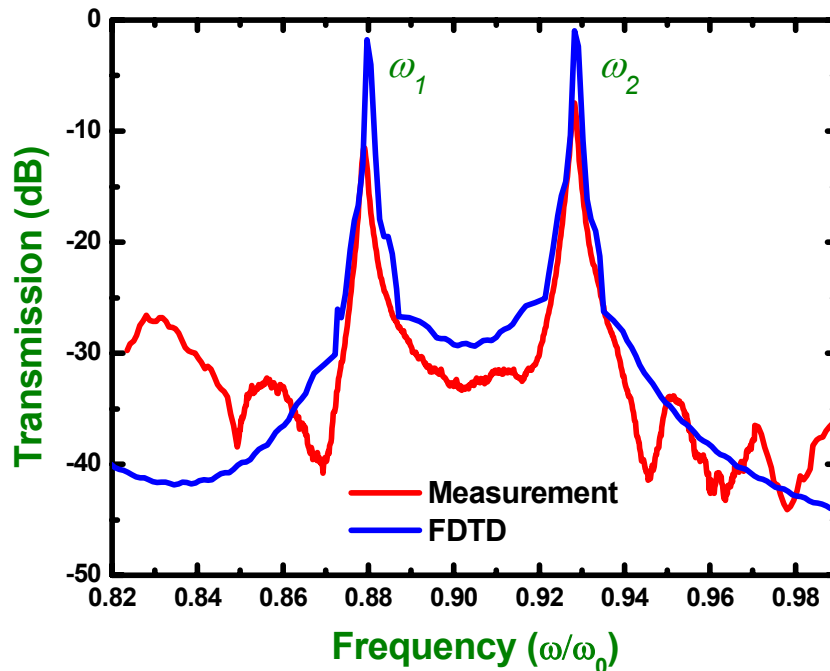


$$\mathbf{E}_\omega(\mathbf{r}) = A\mathbf{E}_\Omega(\mathbf{r}) + B\mathbf{E}_\Omega(\mathbf{r} - \Lambda)$$

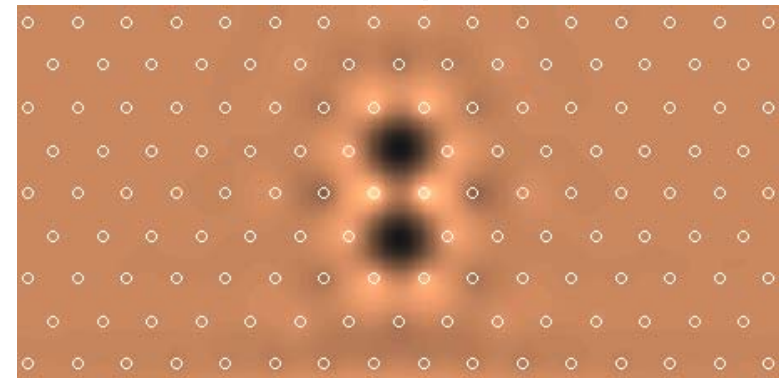
Linear combination of the individual evanescent cavity modes

$$\nabla \times [\nabla \times \mathbf{E}_\omega(\mathbf{r})] = (\omega/c)^2 \epsilon_0(\mathbf{r}) \mathbf{E}_\omega(\mathbf{r})$$

$$\omega_{1,2} = \Omega \sqrt{\frac{1 \pm \beta}{1 \pm \alpha}}$$



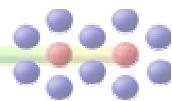
$$E_{\omega_1} = \frac{E_\Omega(\mathbf{r}) - E_\Omega(\mathbf{r} - \Lambda)}{\sqrt{2}}$$



$$E_{\omega_2} = \frac{E_\Omega(\mathbf{r}) + E_\Omega(\mathbf{r} - \Lambda)}{\sqrt{2}}$$

Formation of bonding and antibonding photonic modes

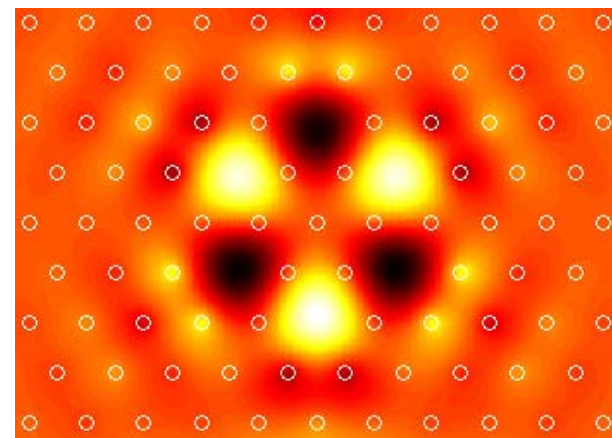
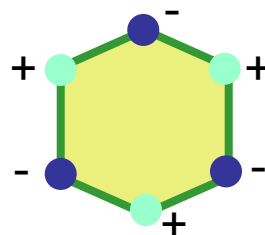
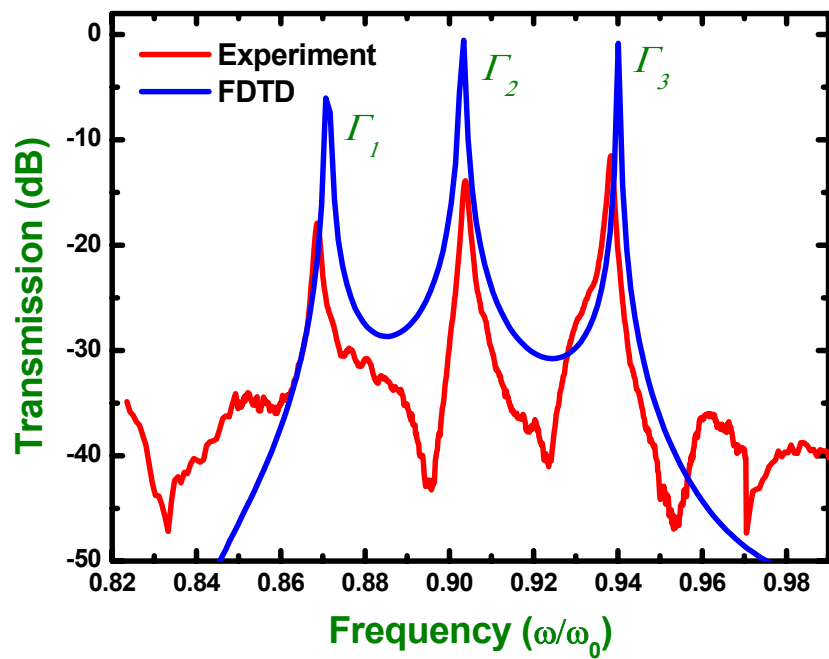
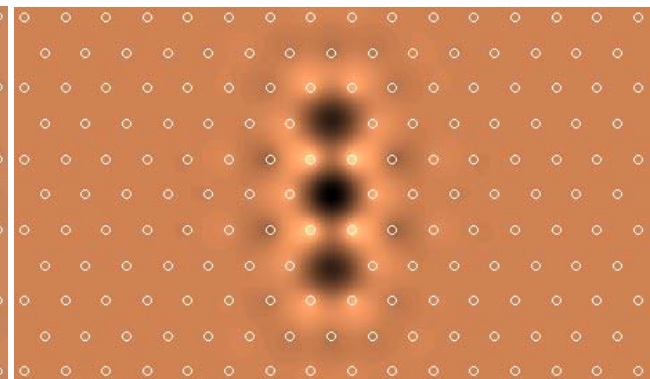
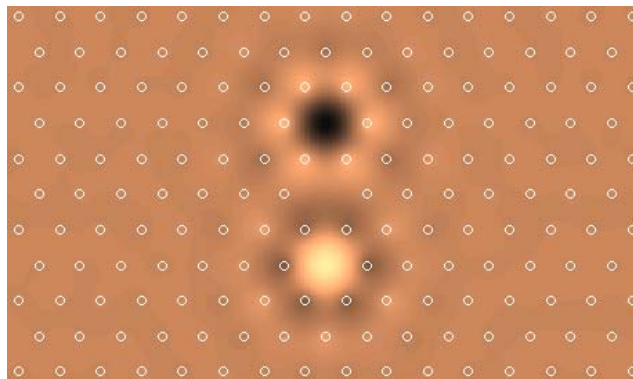
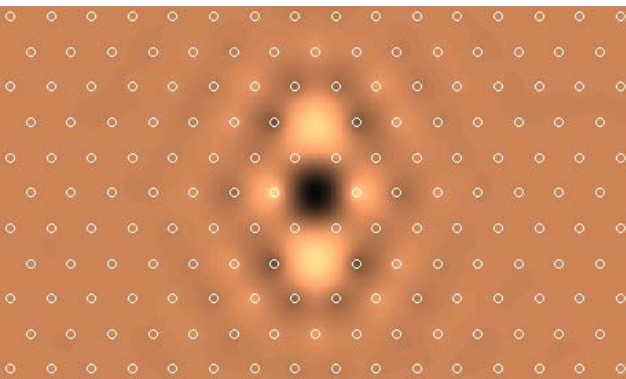
PHOTONIC MOLECULES



$$E_{r_1} = \frac{E_{\Omega}(\mathbf{r}) - \sqrt{2}E_{\Omega}(\mathbf{r}-\mathbf{A}) + E_{\Omega}(\mathbf{r}-2\mathbf{A})}{2}$$

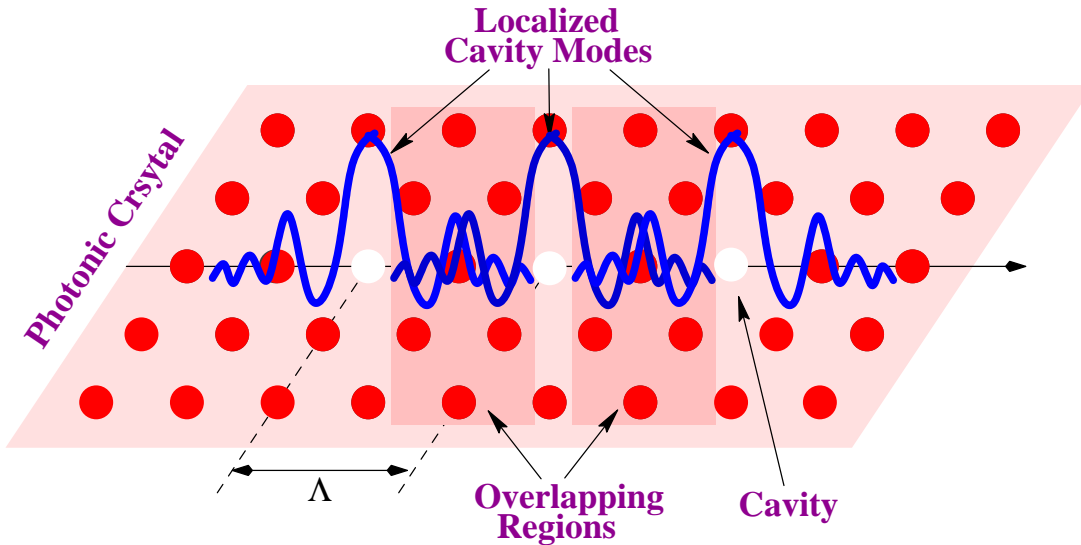
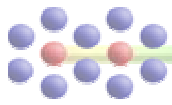
$$E_{r_2} = \frac{E_{\Omega}(\mathbf{r}) - E_{\Omega}(\mathbf{r}-2\mathbf{A})}{\sqrt{2}}$$

$$E_{r_3} = \frac{E_{\Omega}(\mathbf{r}) + \sqrt{2}E_{\Omega}(\mathbf{r}-\mathbf{A}) + E_{\Omega}(\mathbf{r}-2\mathbf{A})}{2}$$



Benzene-like molecule

THE TIGHT-BINDING PICTURE IN PHOTONIC STRUCTURES



✓ highly localized

✓ weakly interacting cavity modes



Tight-binding approximation

Dispersion relation, group velocity, and photon lifetime depend only a single tight-binding parameter κ that can be directly determined from experiments

$$\nabla \times [\nabla \times \mathbf{E}(\mathbf{r})] = (\omega/c)^2 \varepsilon_0(\mathbf{r}) \mathbf{E}(\mathbf{r})$$

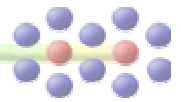
$$\mathbf{E}(\mathbf{r}) = E_0 \sum_n e^{-ink\Lambda} \mathbf{E}_\Omega(\mathbf{r} - n\Lambda)$$

$$\omega(k) = \Omega(1 + \kappa \cos(k\Lambda))$$

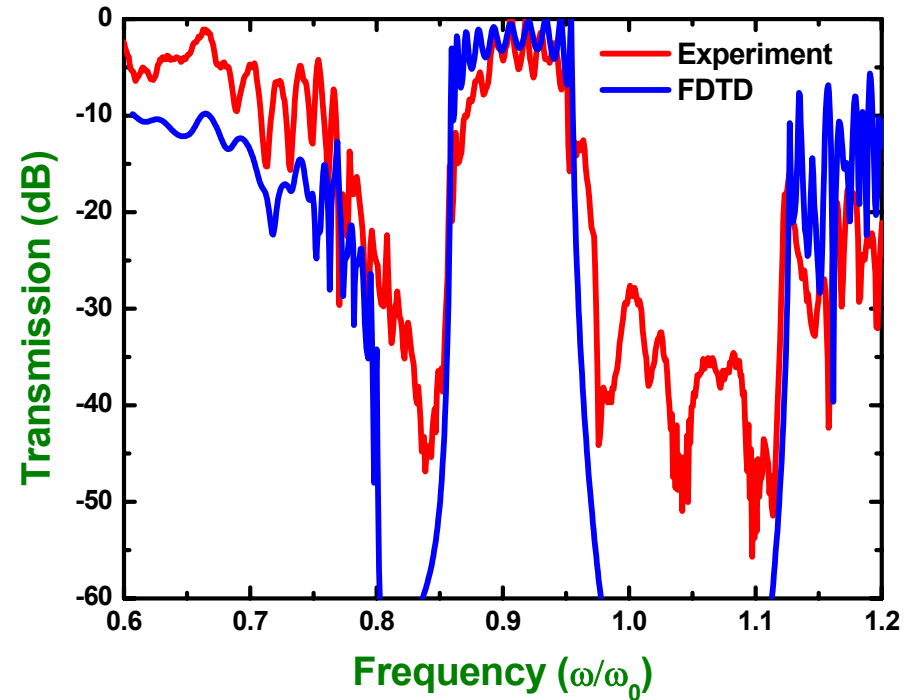
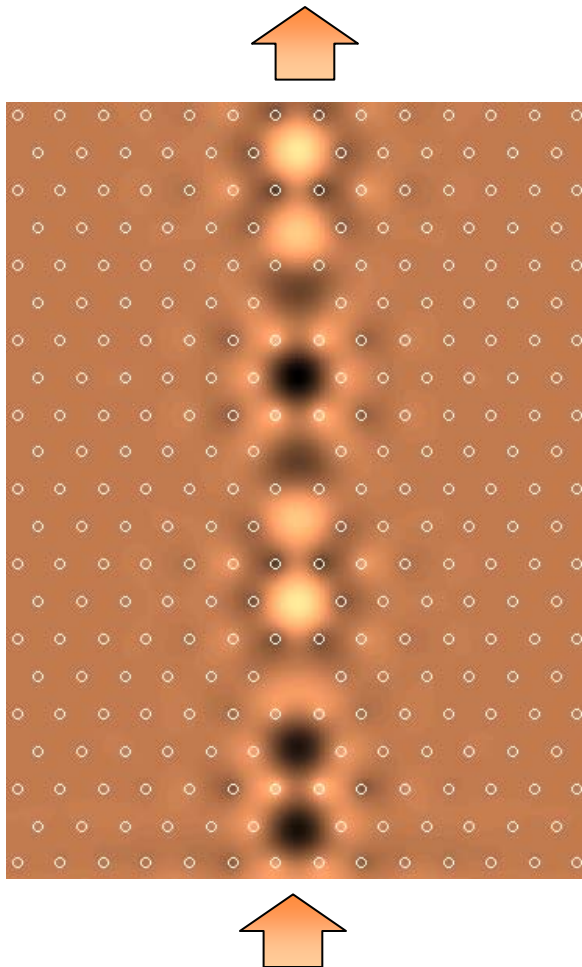
$$v_g(k) = \nabla_k \omega(k) = -\Omega\Lambda\kappa \sin(k\Lambda)$$

$$\tau_p(k) = L/v_g(k) - 2\pi L/c$$

PROPAGATION OF PHOTONS BY HOPPING

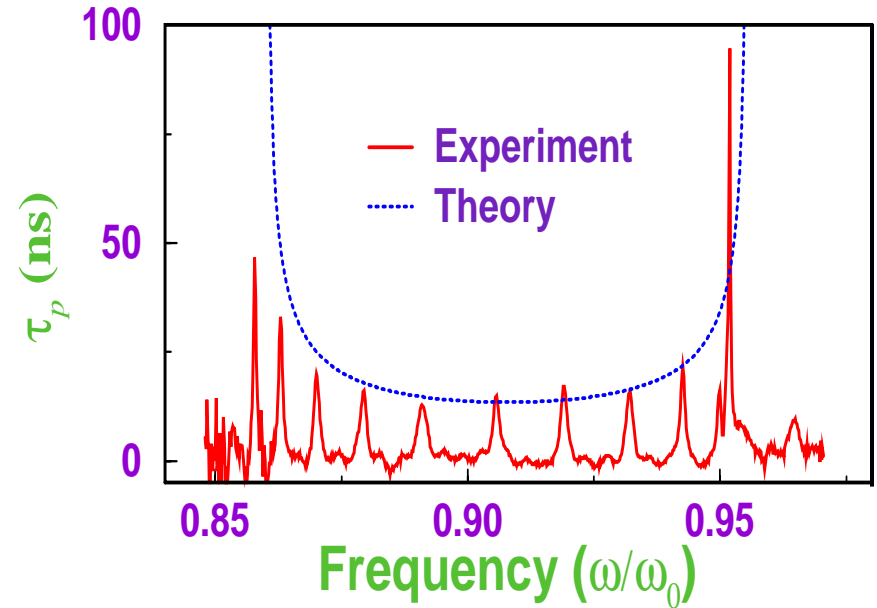
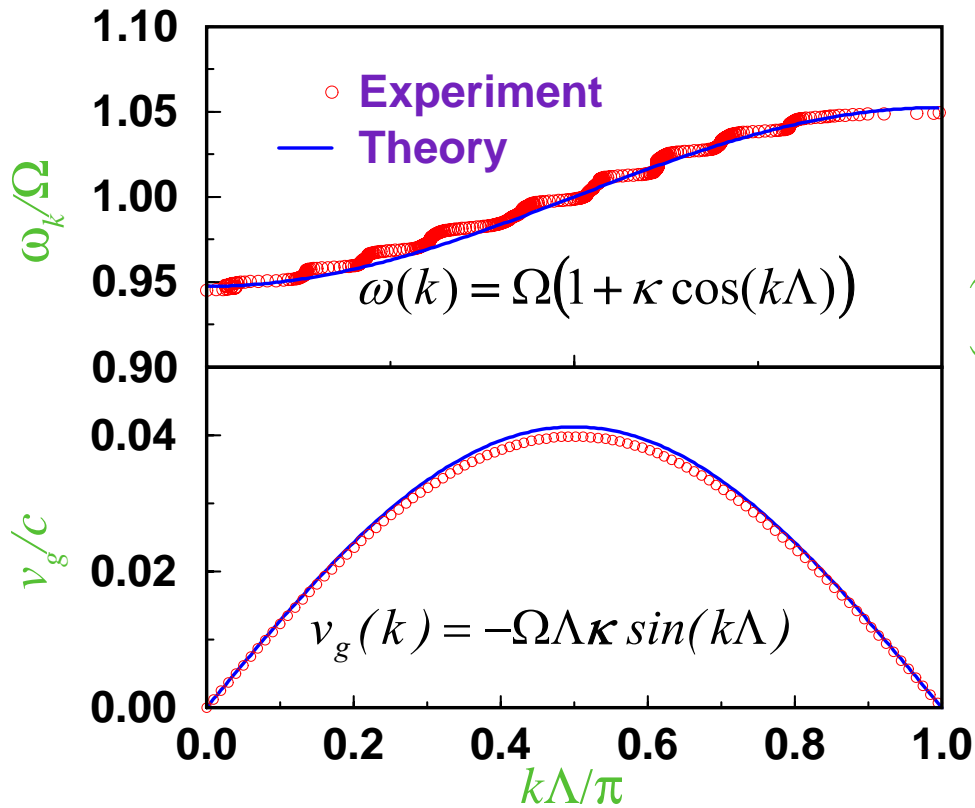
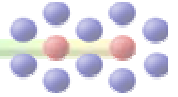


Straight Waveguide



- Formation of a cavity band (waveguiding band) due to interaction between the localized modes
- Demonstration of a new type of waveguiding mechanism in photonic crystals.
 - Full transmission is measured throughout the CCW band
 - Very sharp band edges can be used for switching applications

DISPERSION RELATION, GROUP VELOCITY, PHOTON LIFETIME: MEASUREMENTS AND CALCULATIONS



$$\tau_p(k) = L/v_g(k) - 2\pi L/c$$

$$v_g \rightarrow 0$$

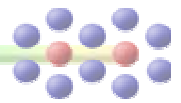
$$\tau_p \rightarrow \infty$$

at the CCW band edges

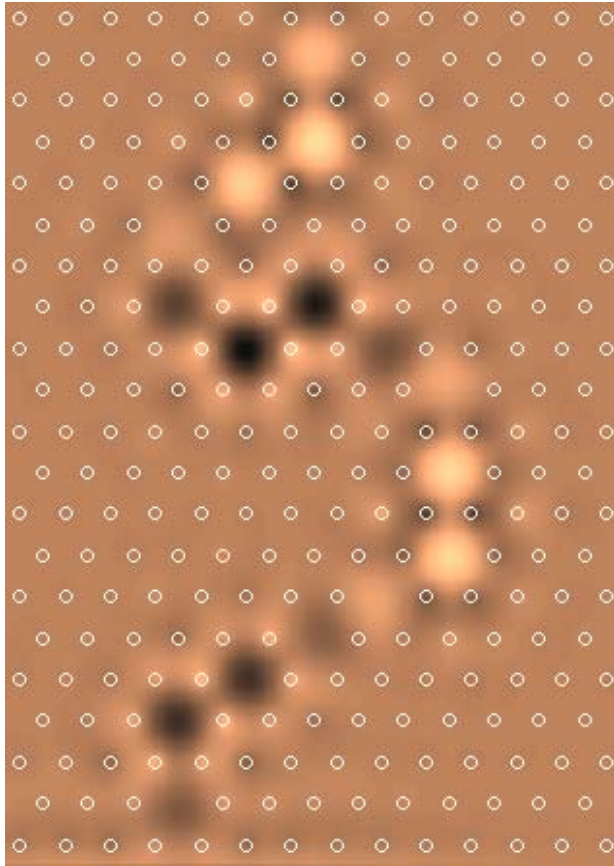


“heavy photon”

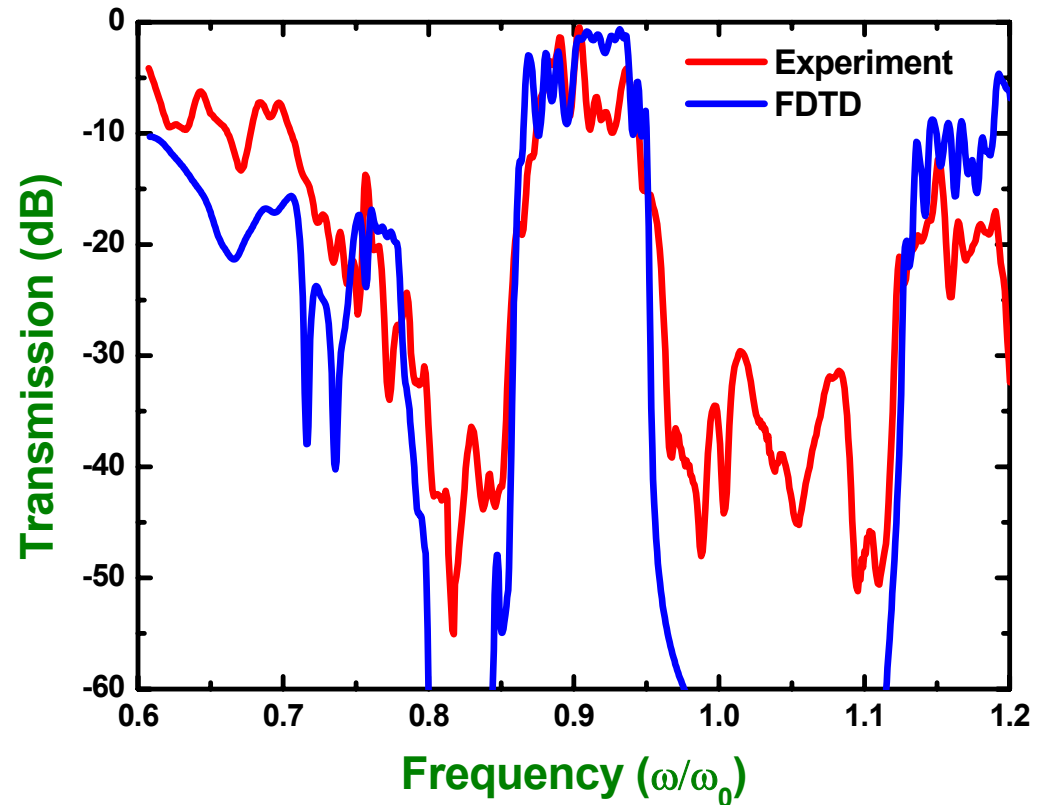
BENDING OF EM WAVES ALONG ARBITRARY PATH



Zig-zag Waveguide

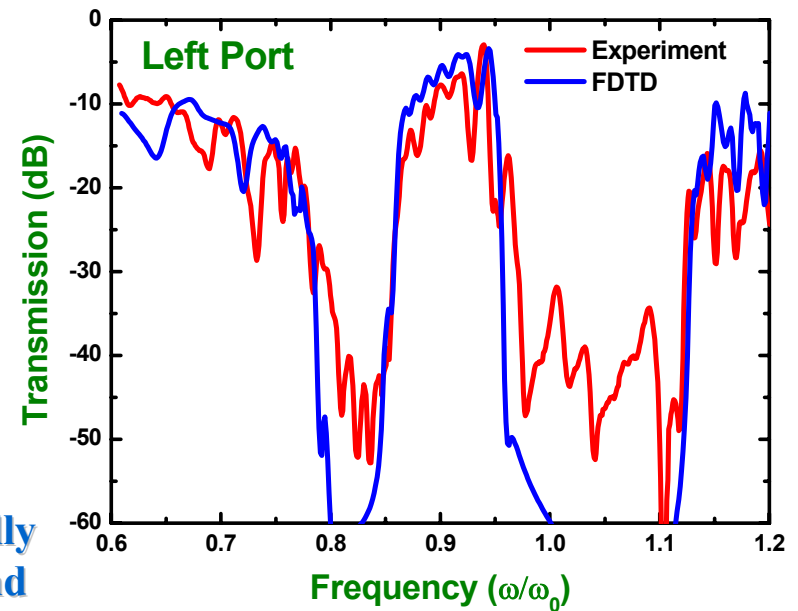
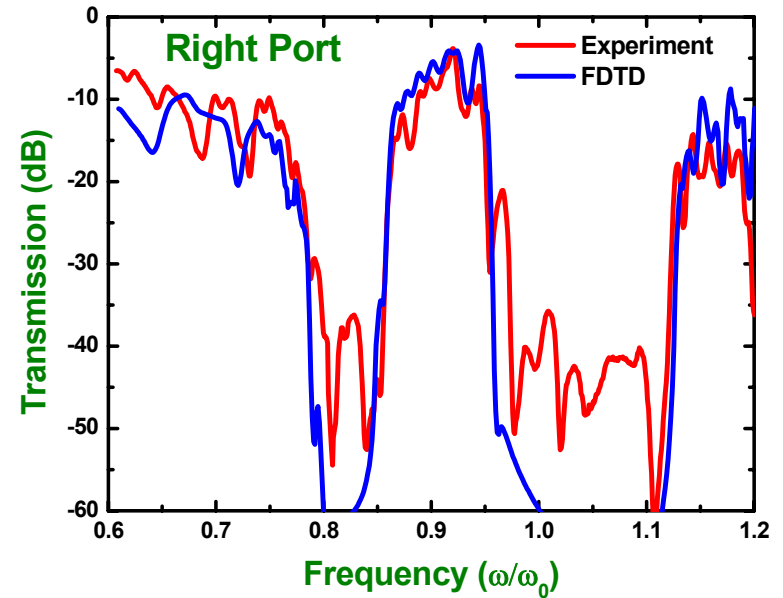
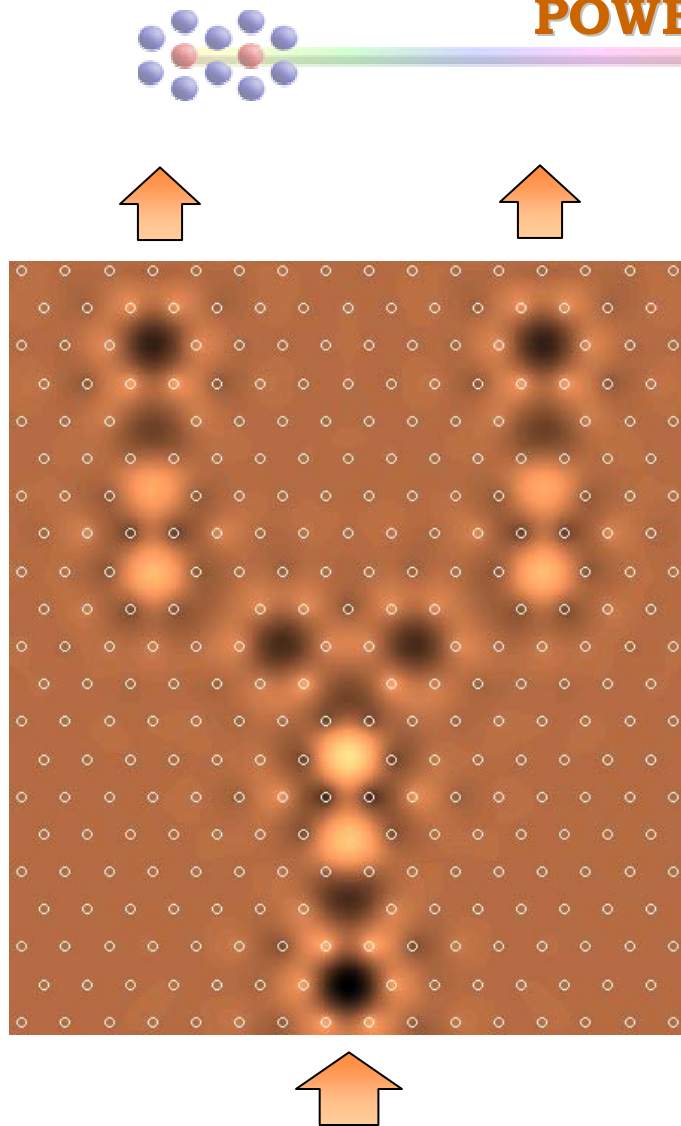


Problem of guiding light
around very sharp corners
in conventional waveguides



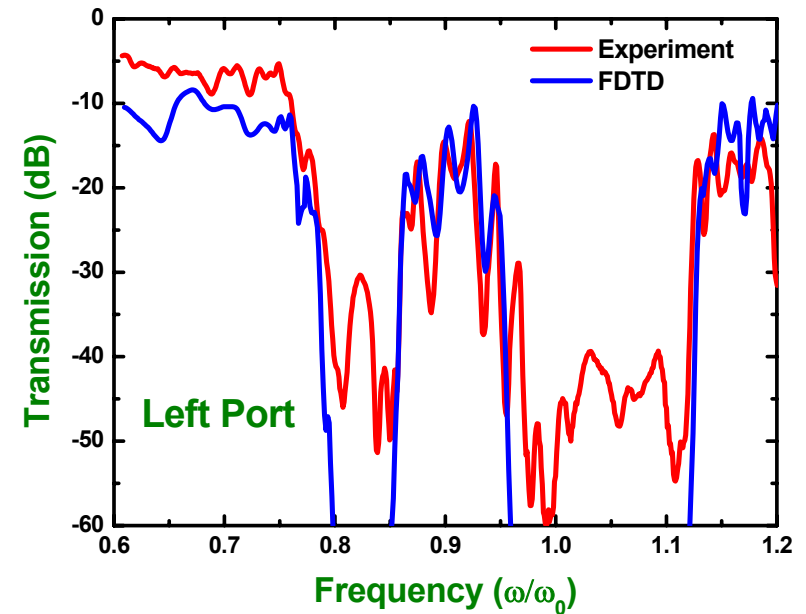
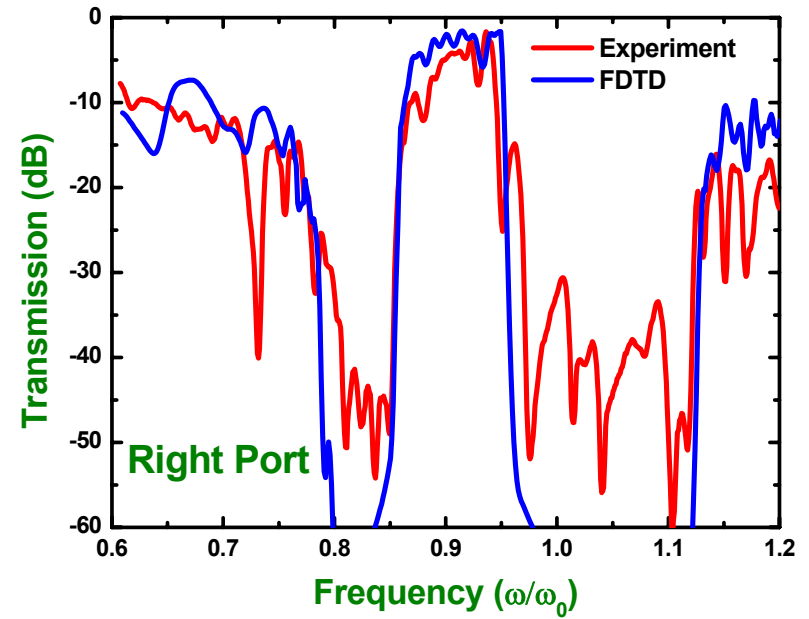
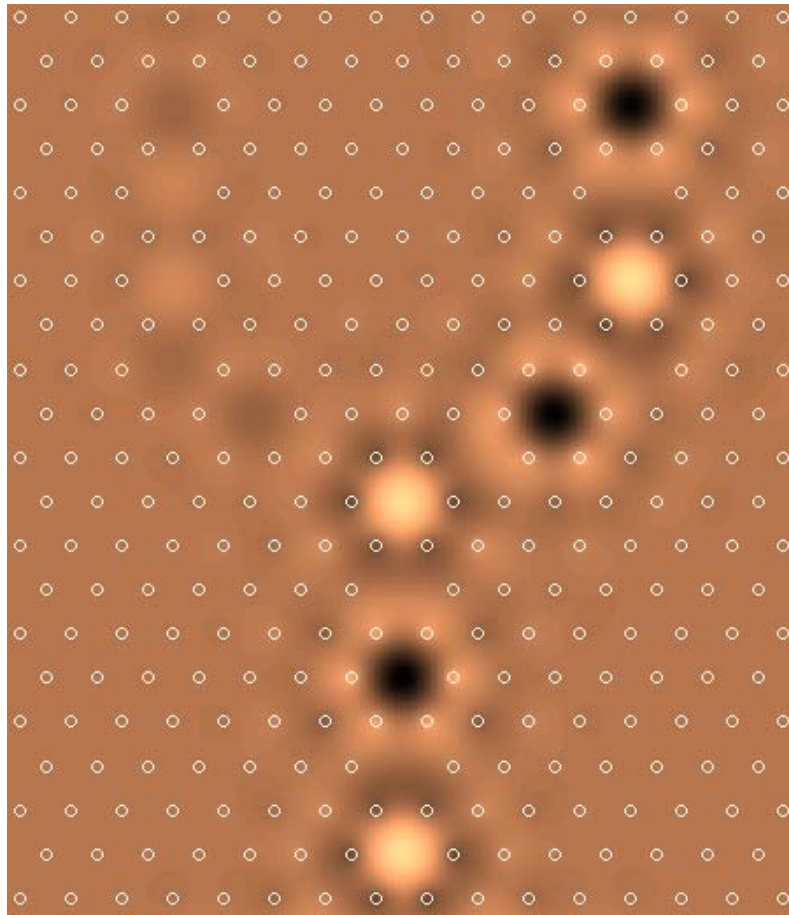
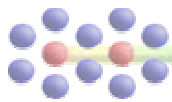
➤ Possibility of constructing lossless and reflectionless bends in optical circuits

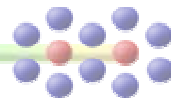
POWER SPLITTERS



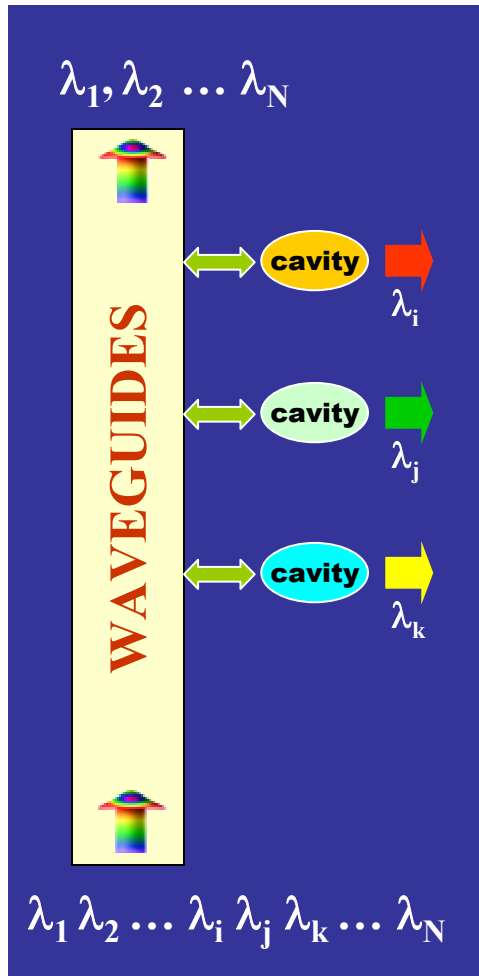
➤ The electromagnetic power in the input port splits equally into the two output ports throughout the waveguiding band

COUPLED CAVITY SWITCHES

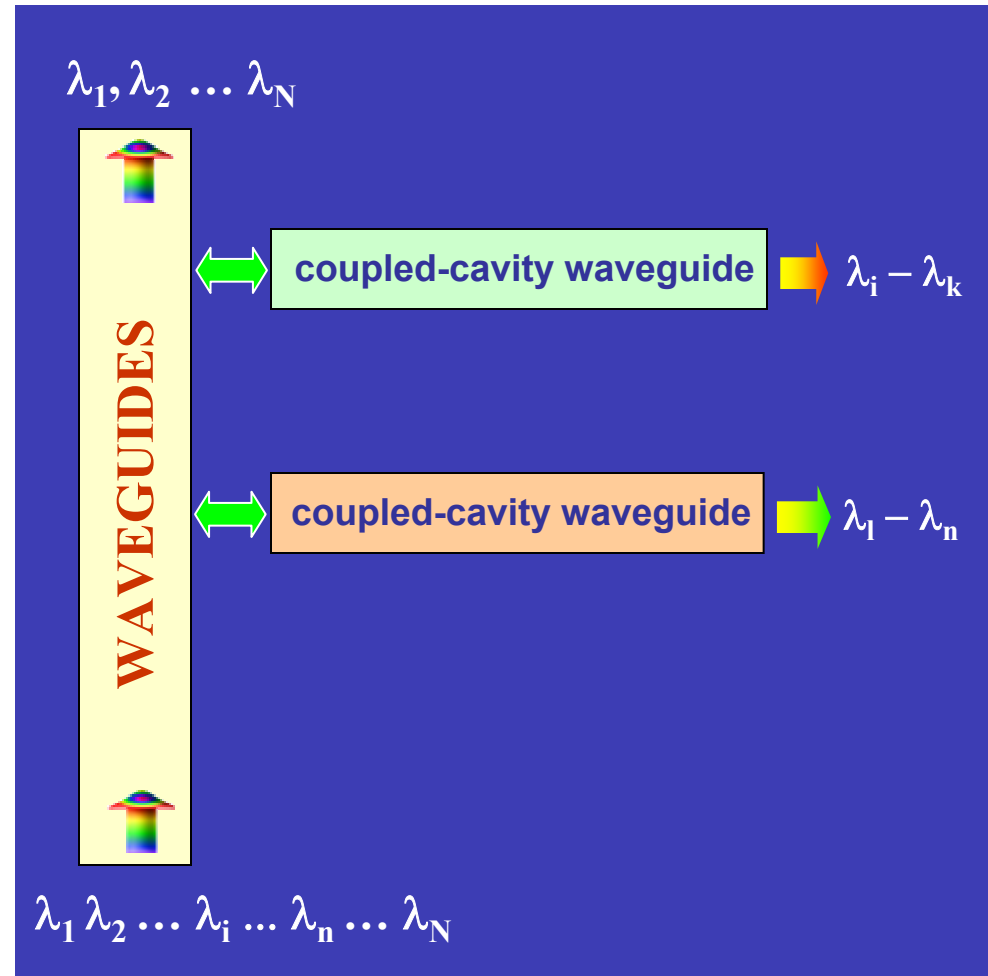




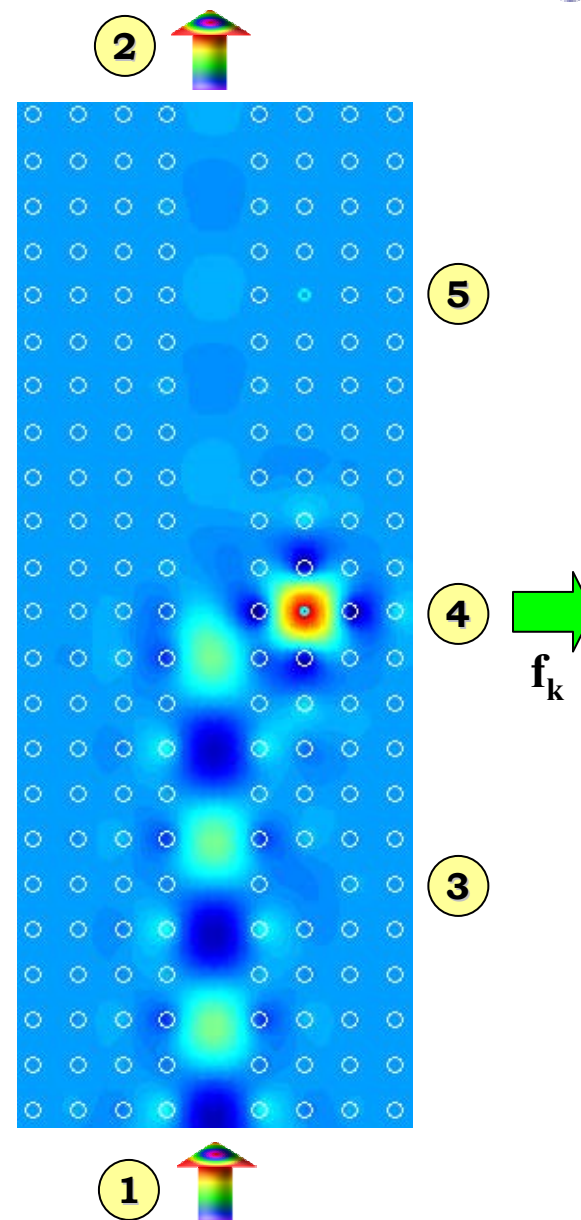
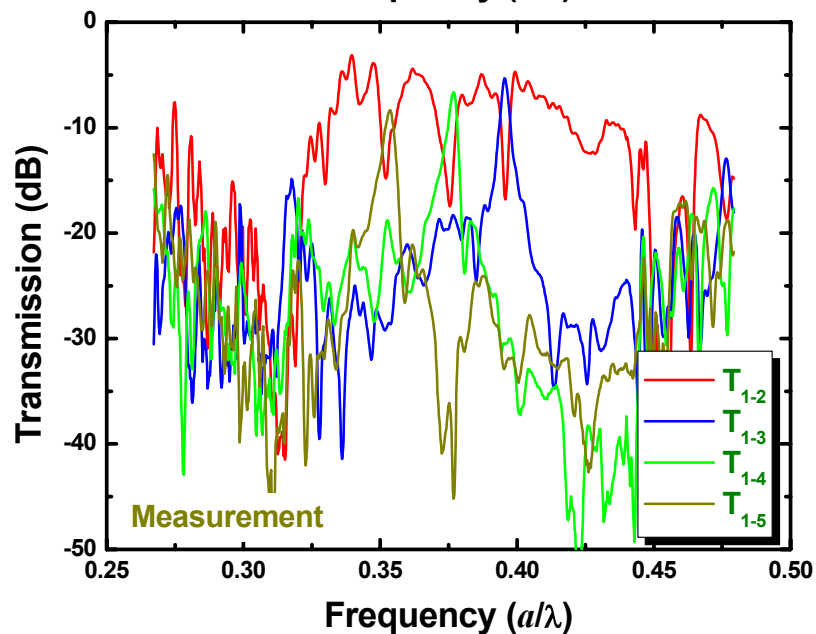
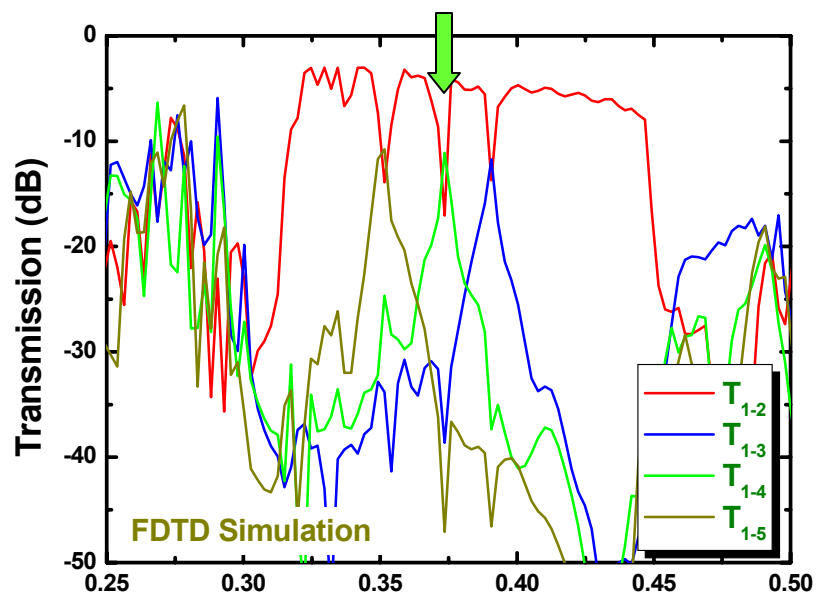
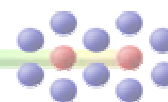
Single wavelength dropping



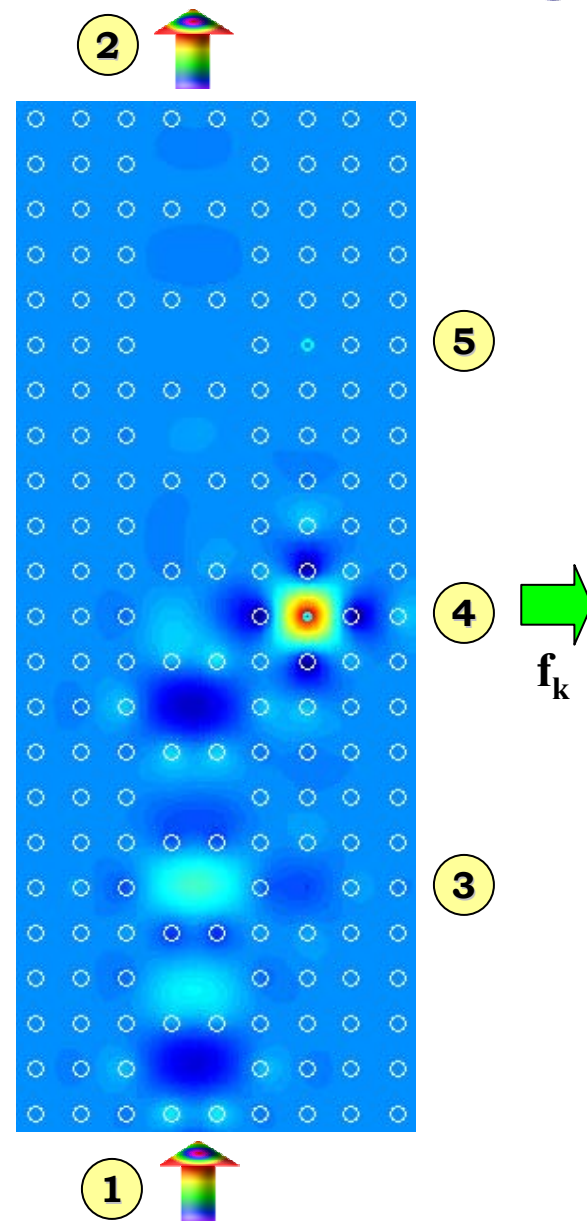
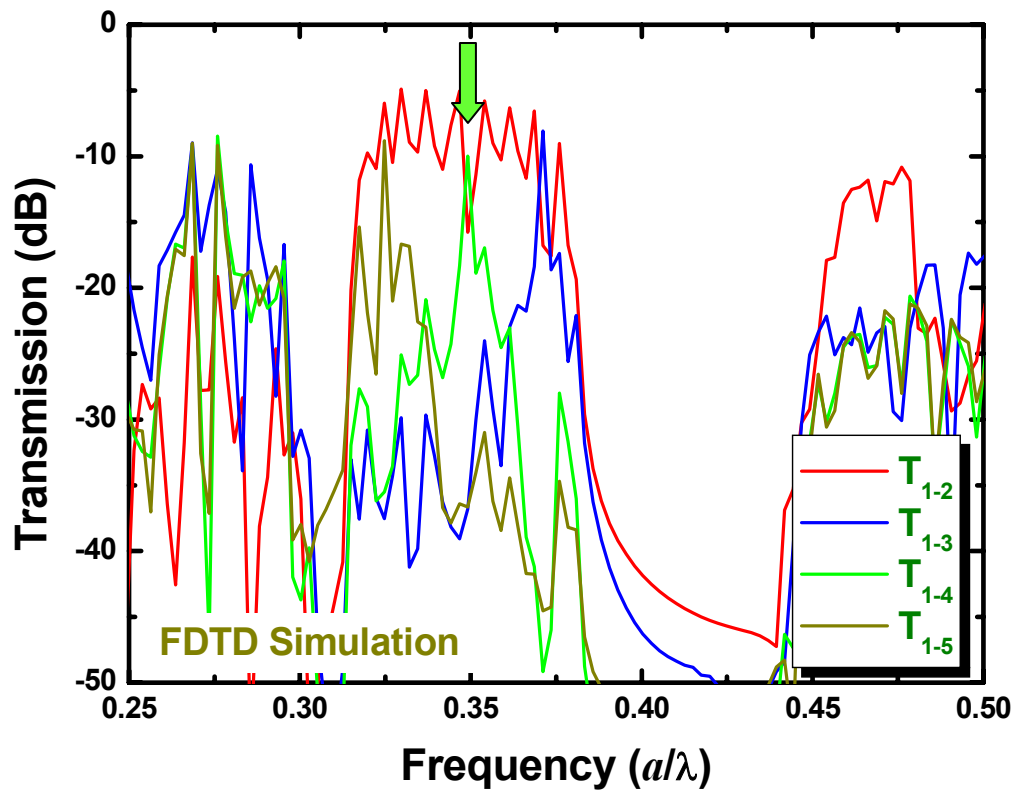
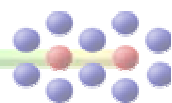
Band dropping



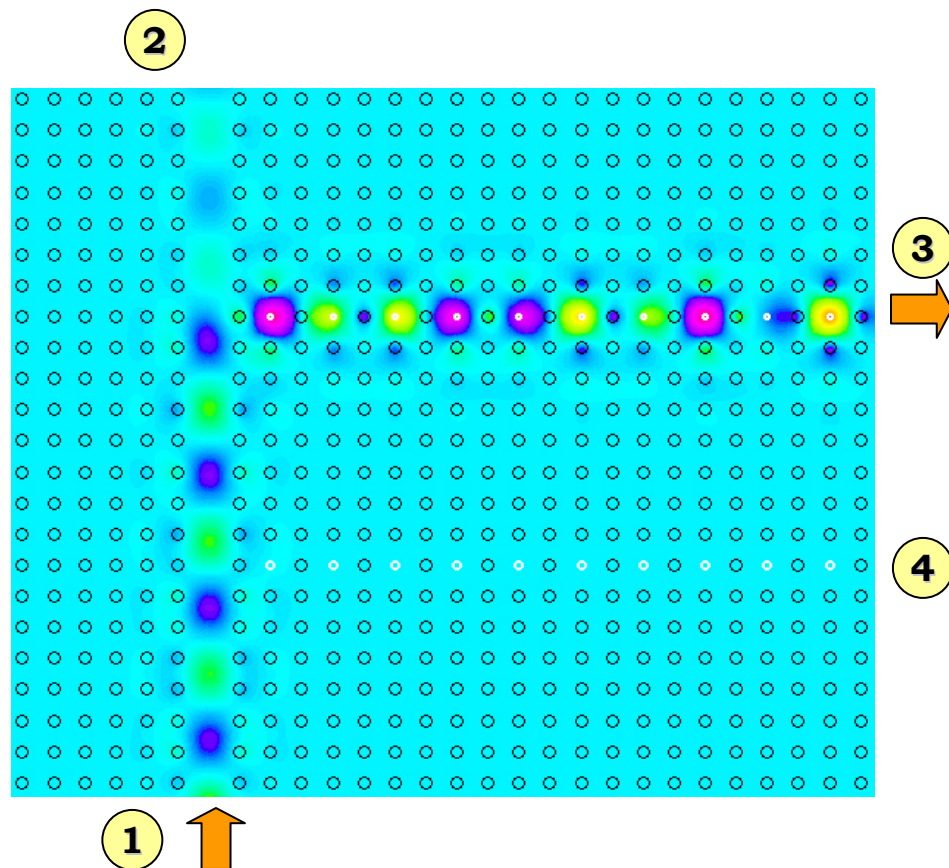
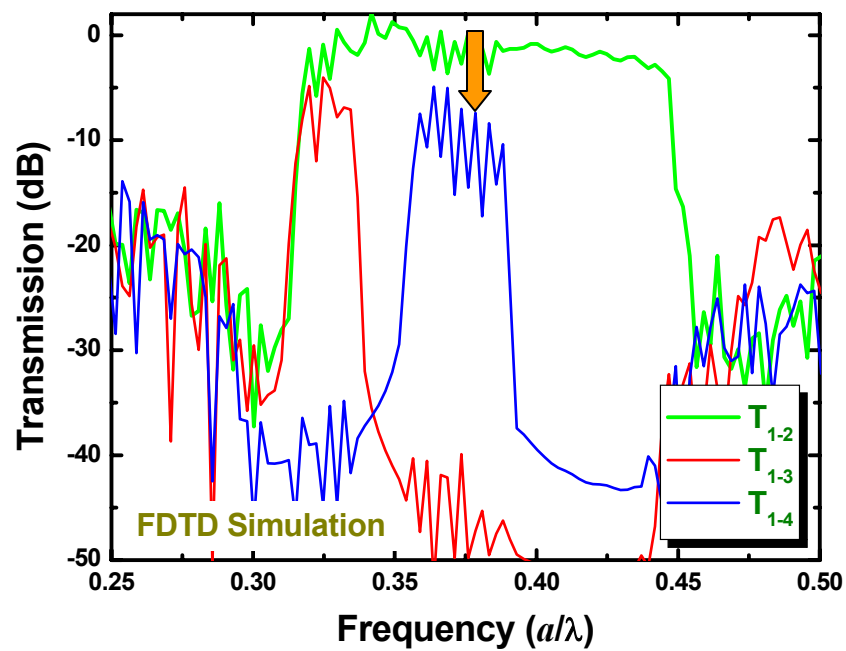
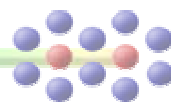
DROPPING OF A SELECTIVE FREQUENCY FROM PW



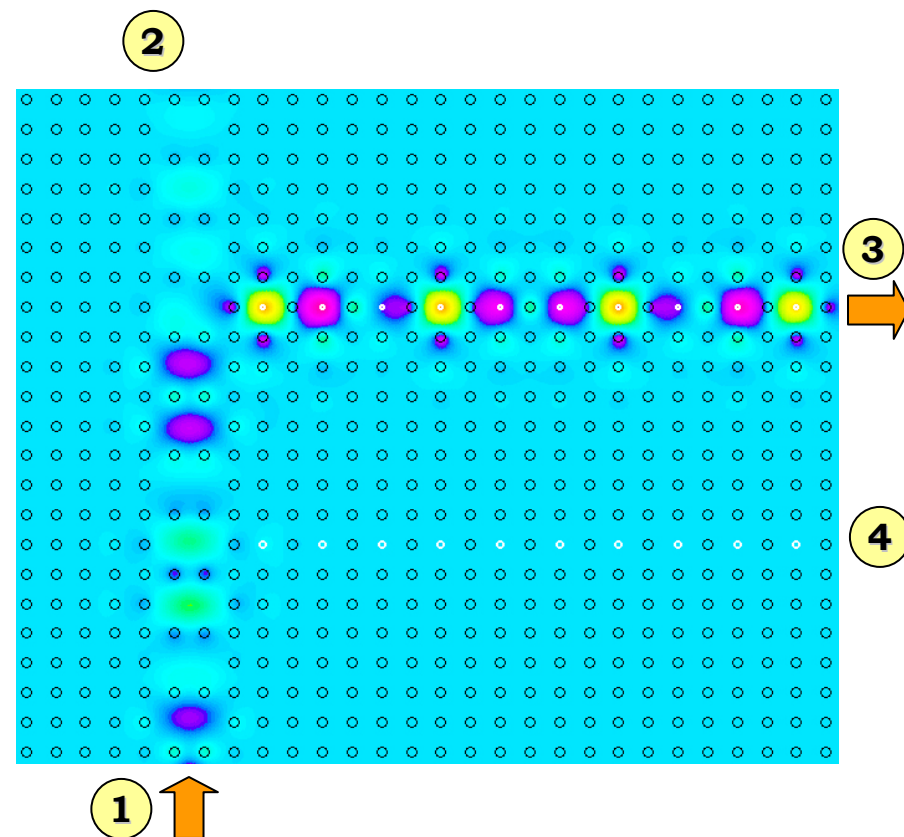
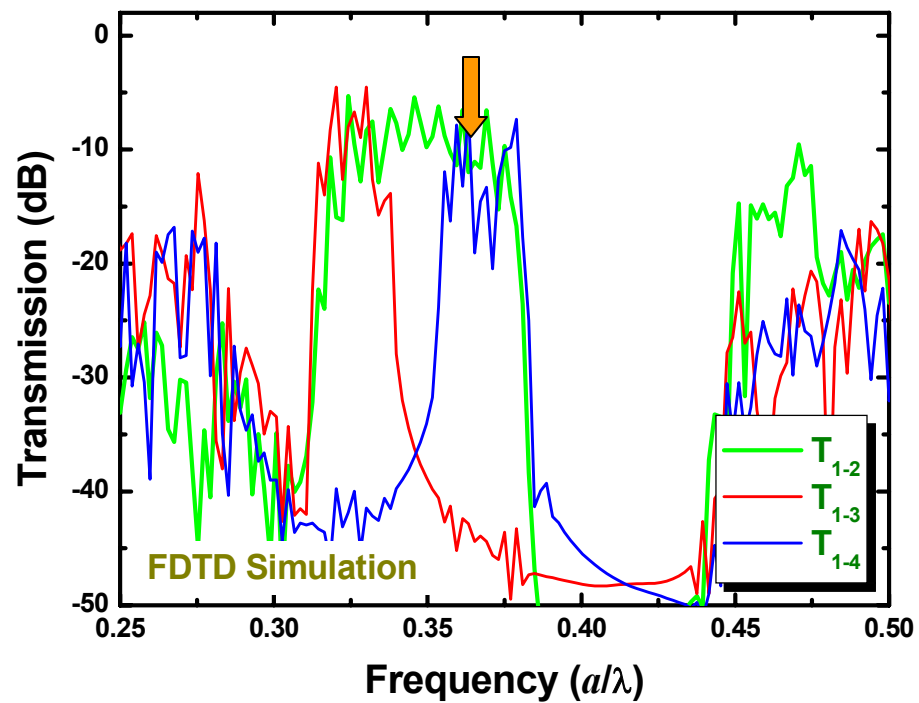
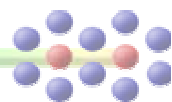
DROPPING OF A SELECTIVE FREQUENCY FROM CCW



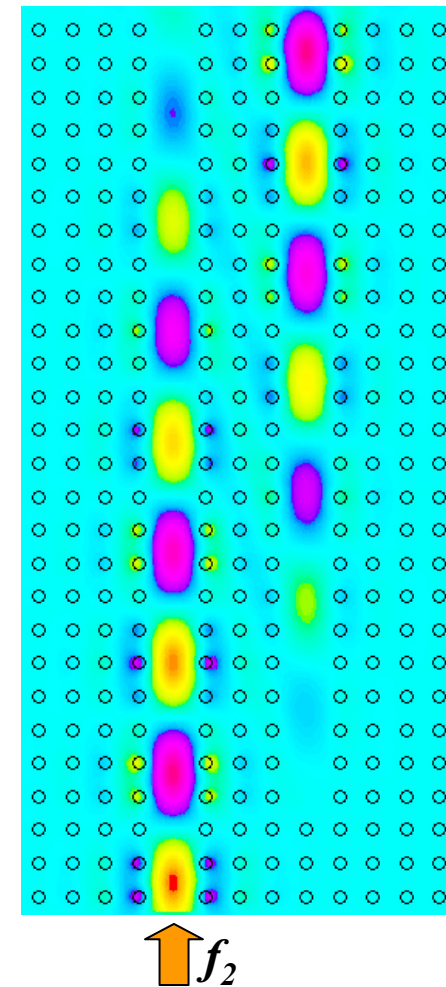
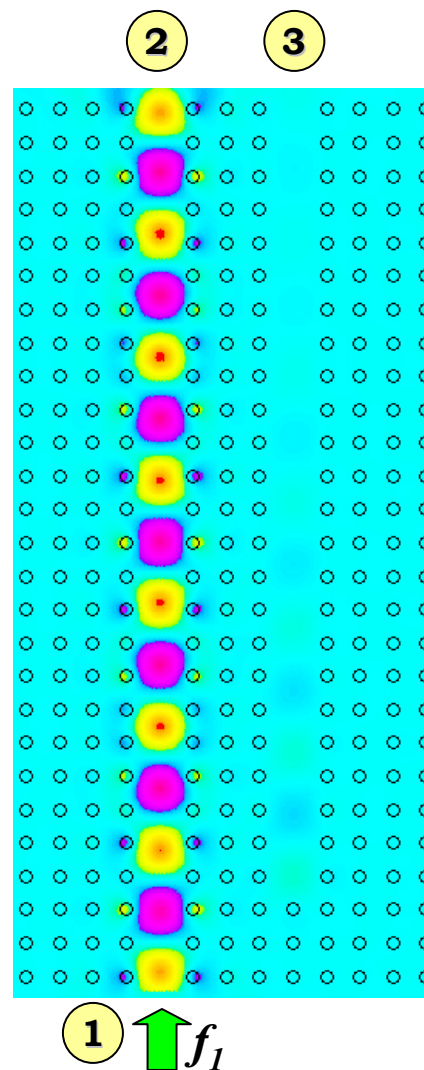
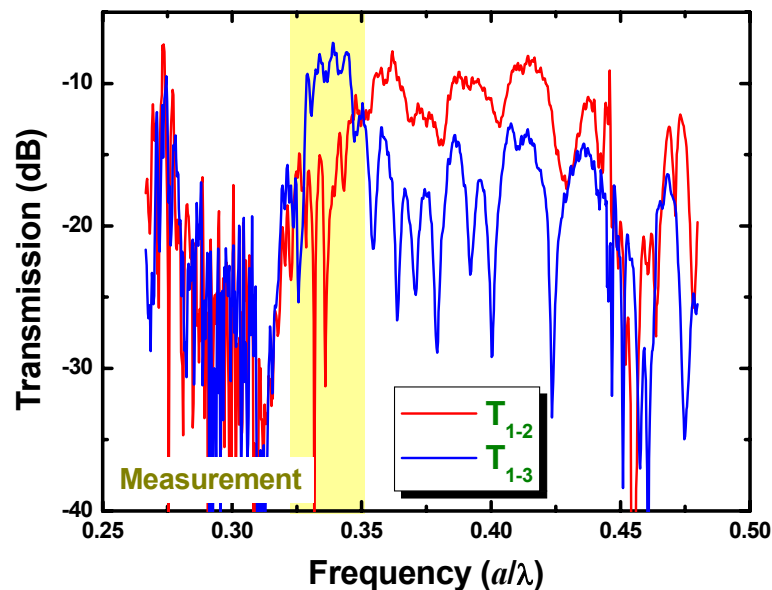
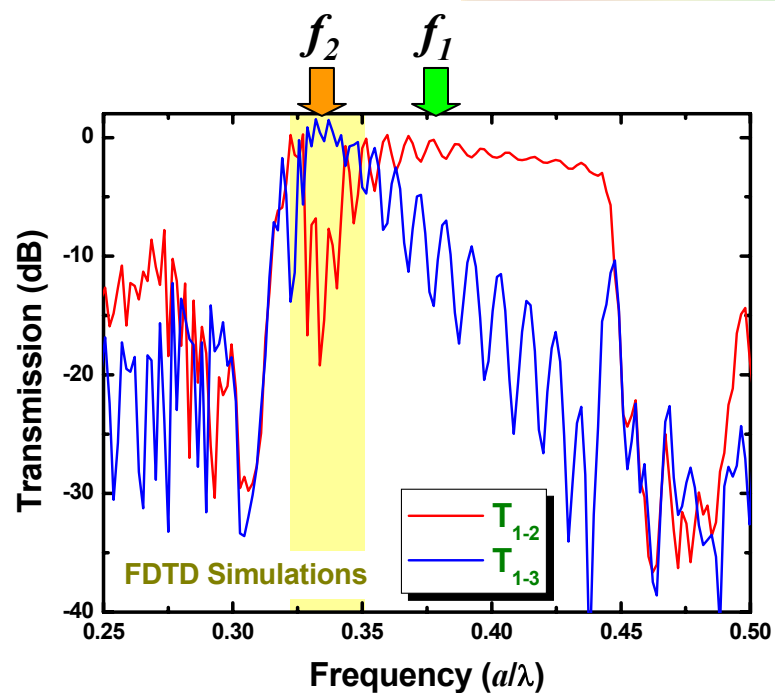
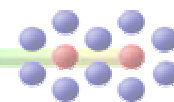
BAND DROPPING FROM PW



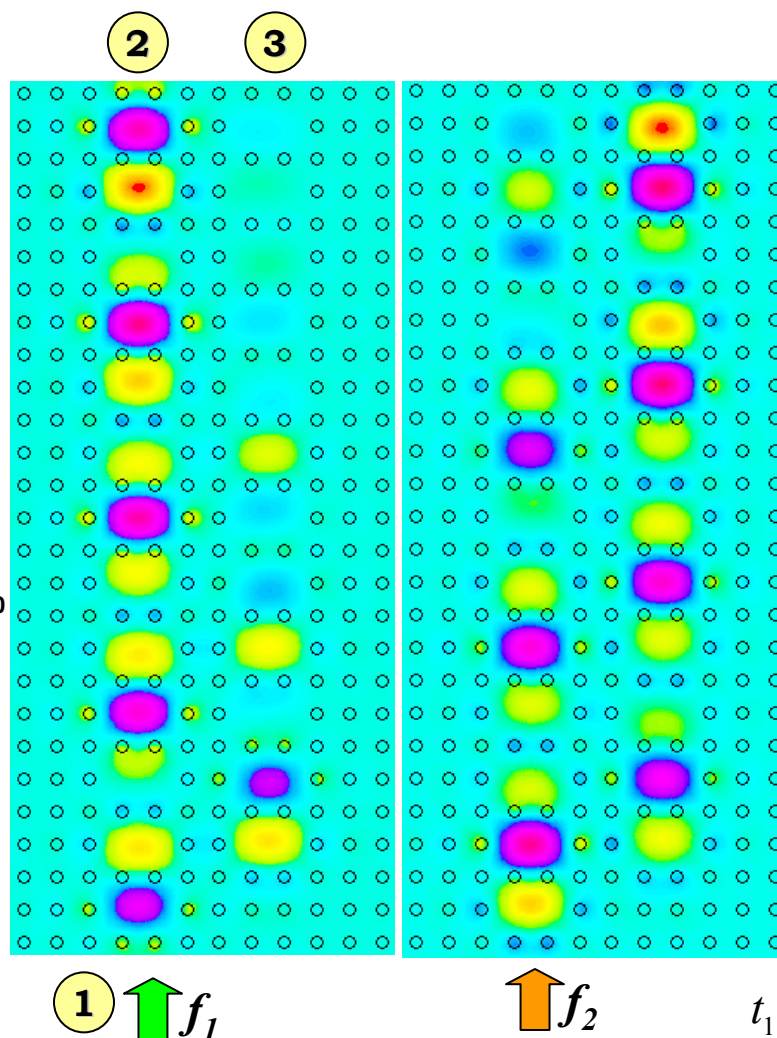
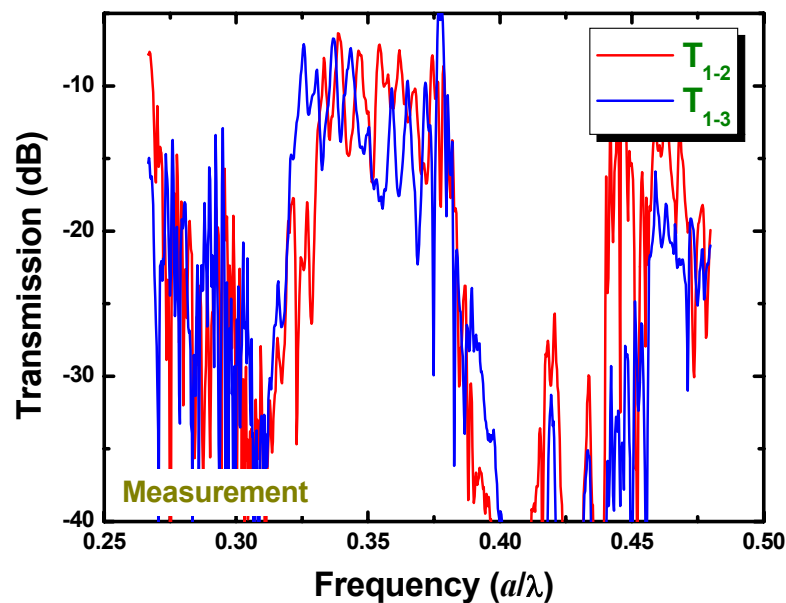
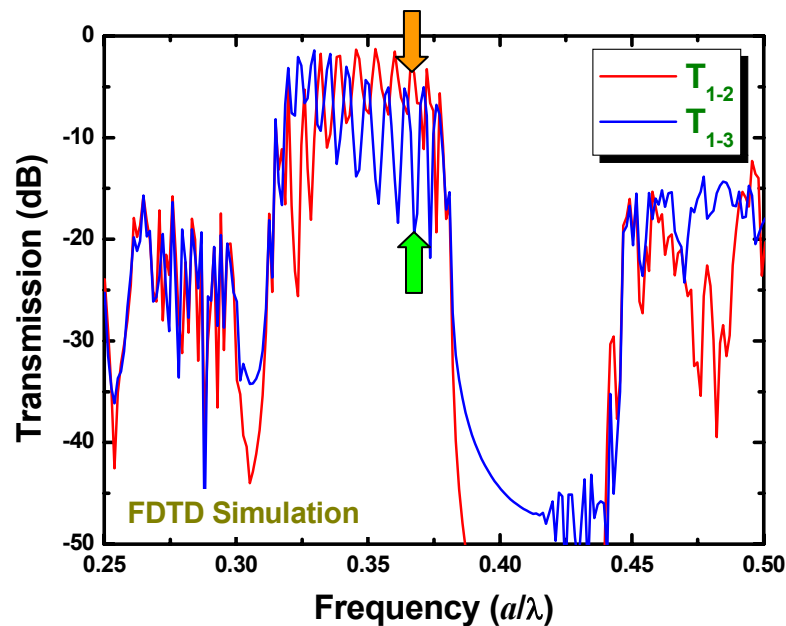
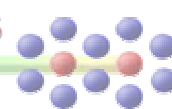
BAND DROPPING FROM CCW



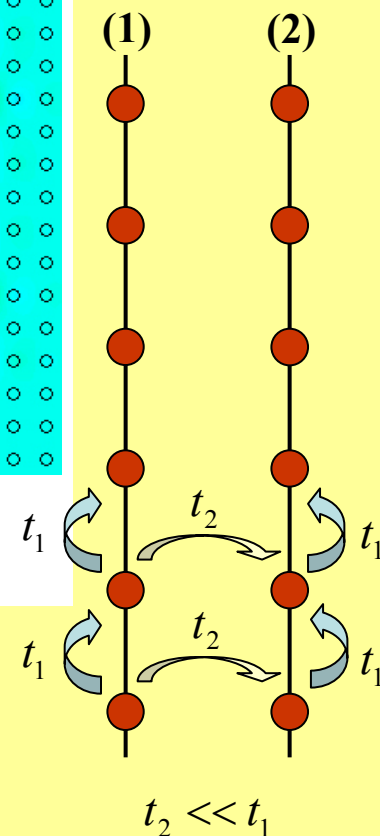
COUPLED WAVEGUIDES: DIRECTIONAL COUPLERS

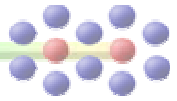


DIRECTIONAL COUPLERS: COUPLED-CAVITY WAVEGUIDES



**TIGHT-BINDING MODEL:
INTERACTING CHAINS**

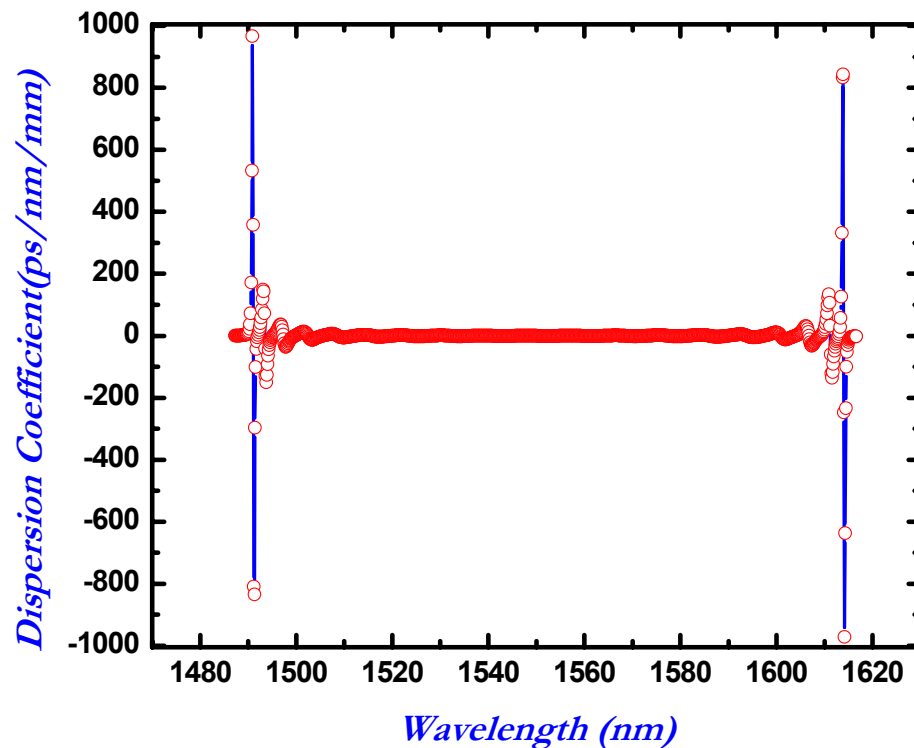




INCREASING EFFICIENCY OF NONLINEAR PROCESSES

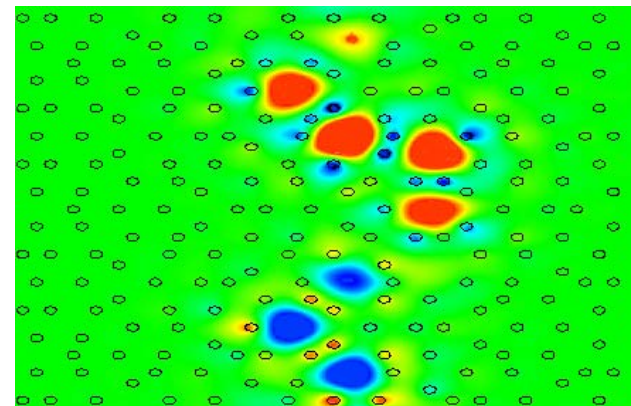
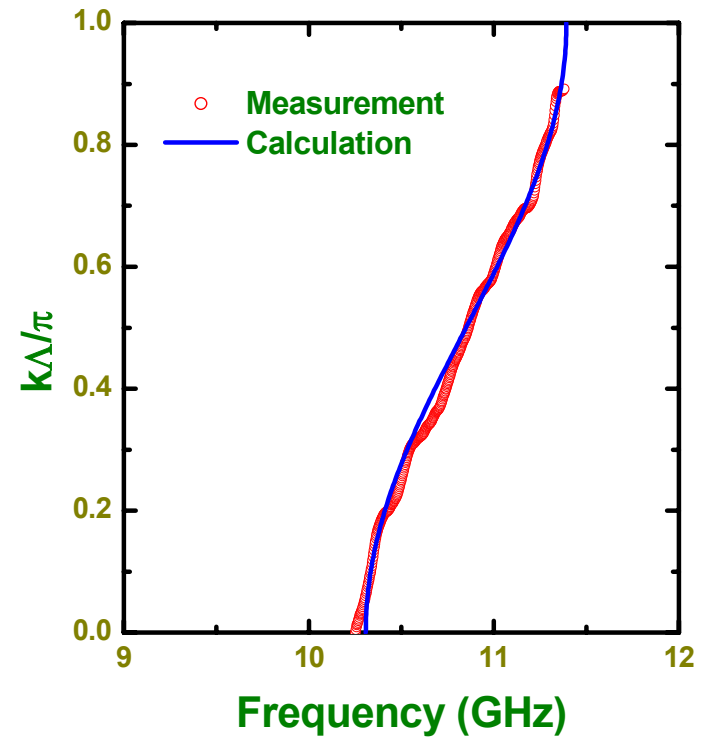
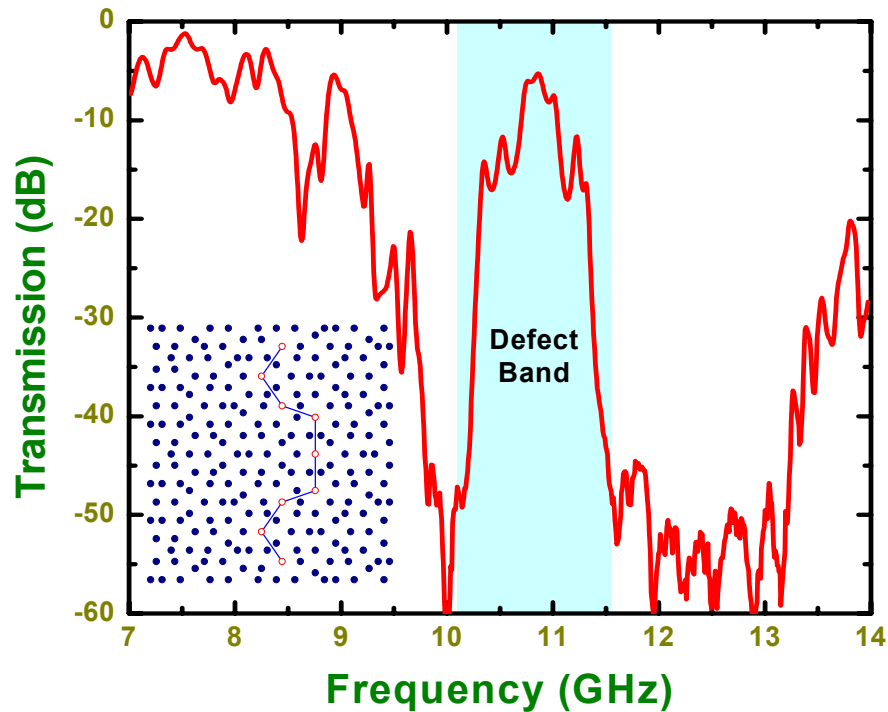
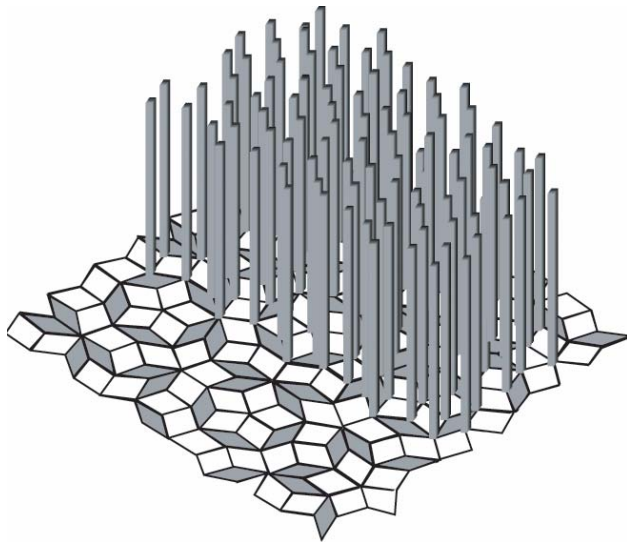
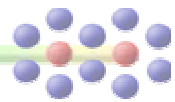
$$\eta \propto 1 / v_g \quad v_g \rightarrow 0 \quad \Rightarrow \quad \text{Large gain}$$

DISPERSION COMPENSATORS

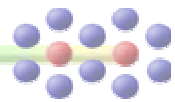


$$D = -\frac{2\pi c}{\lambda^2} \frac{d^2 k}{d\omega^2}$$

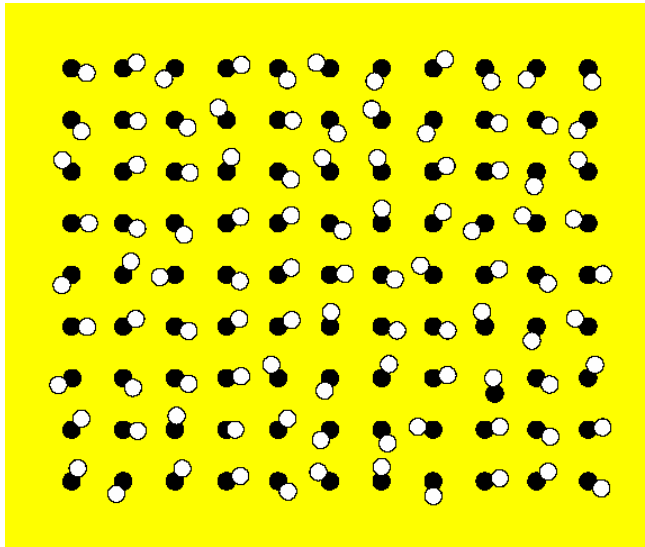
QUASIPERIODIC [PENROSE] PHOTONIC CRYSTALS



COUPLED-CAVITIES IN DISORDERED CRYSTALS



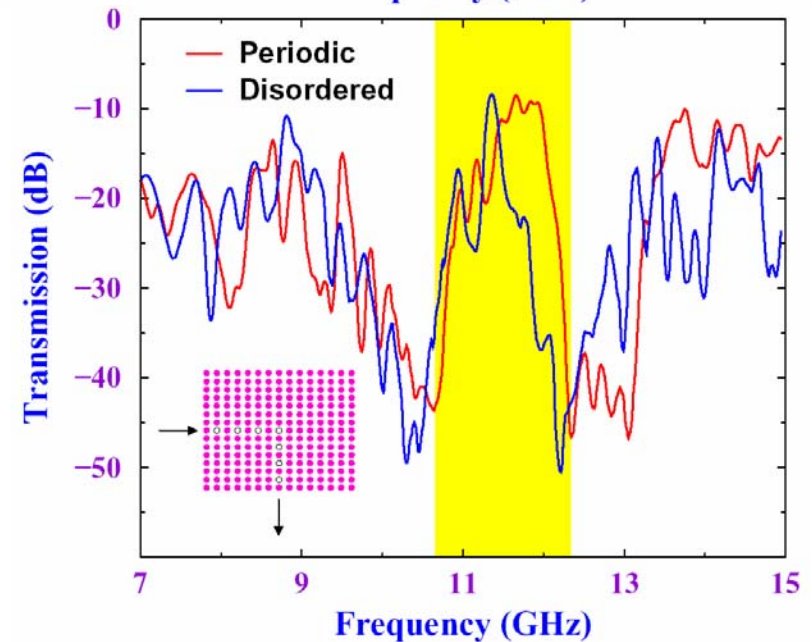
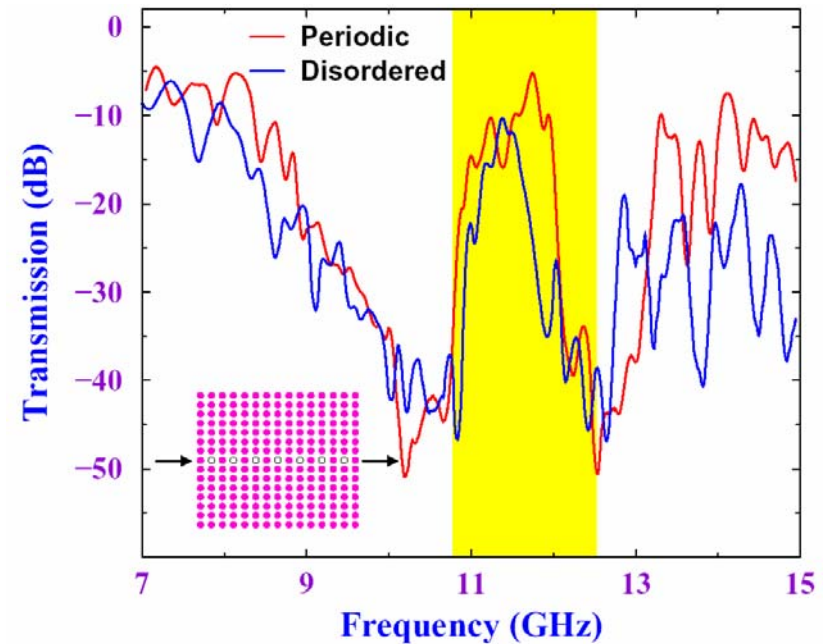
- periodic photonic crystal
- disordered photonic crystal



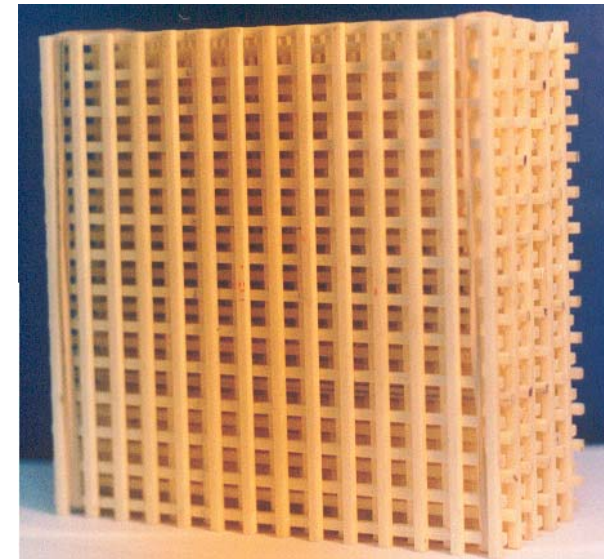
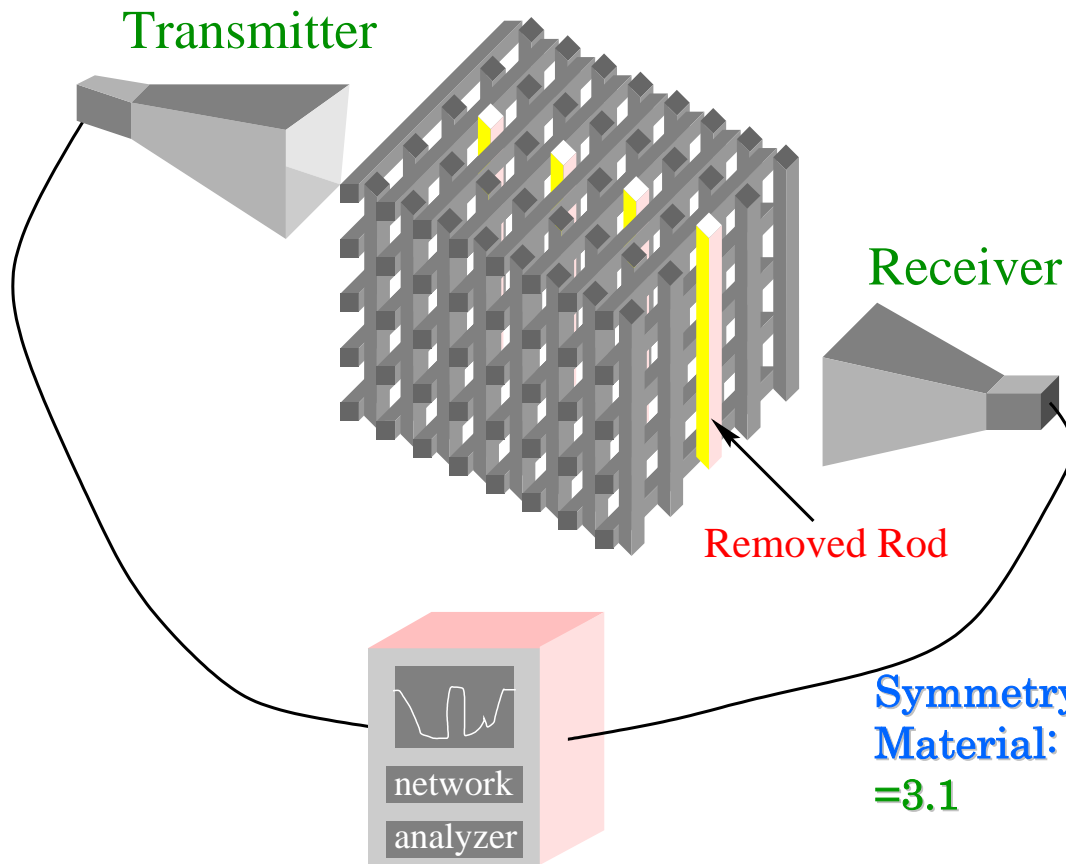
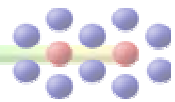
$$z_i \rightarrow z_i r e^{i\varphi}$$

r : randomness parameter

φ : random variable between $[0, \pi]$



3D LAYER-BY-LAYER PHOTONIC CRYSTALS



Symmetry: Face centered tetragonal (fct)
Material: Alumina of refractive index $\epsilon = 3.1$

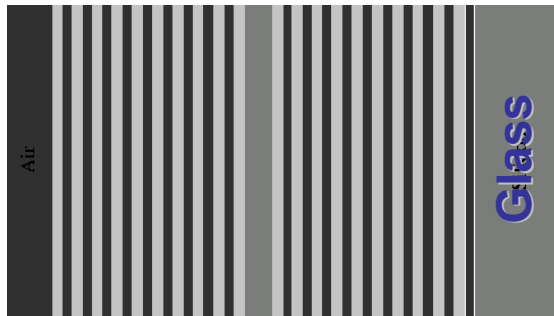
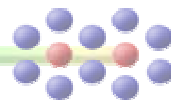
at microwave frequencies

Dimensions: 0.32 cm \times 0.32 cm \times 15.25 cm

Three-dimensional stop band: from 10.6 GHz to 12.8 GHz

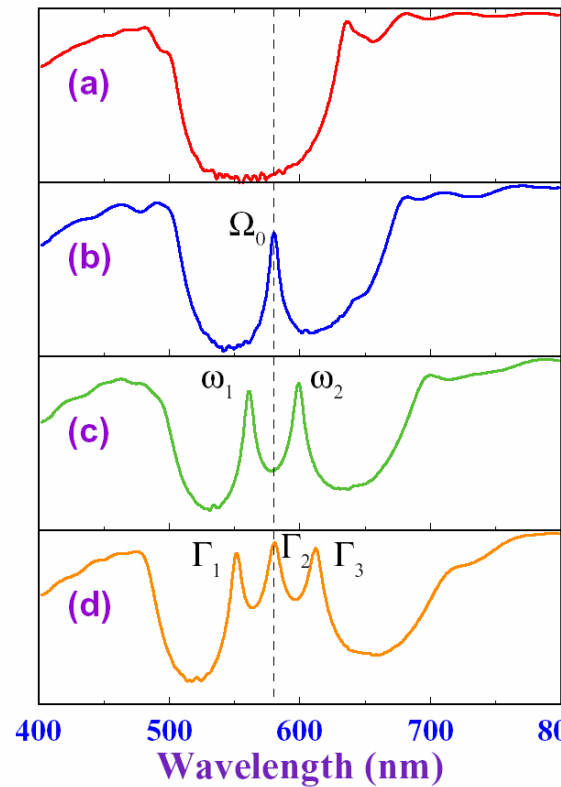
All phenomenon were observed in 3D layer-by-layer or woodpile structures

COUPLED-CAVITIES IN 1D STRUCTURES

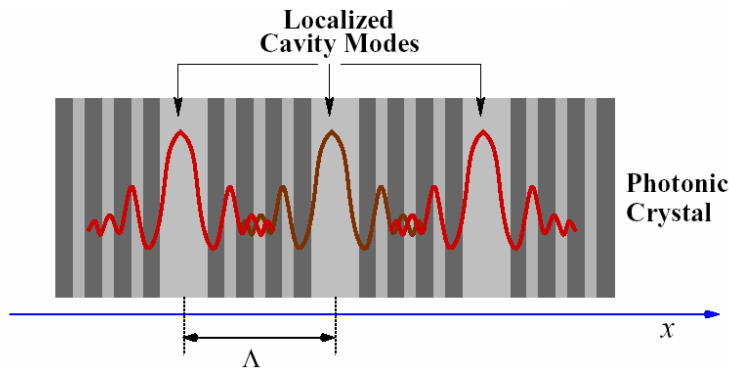
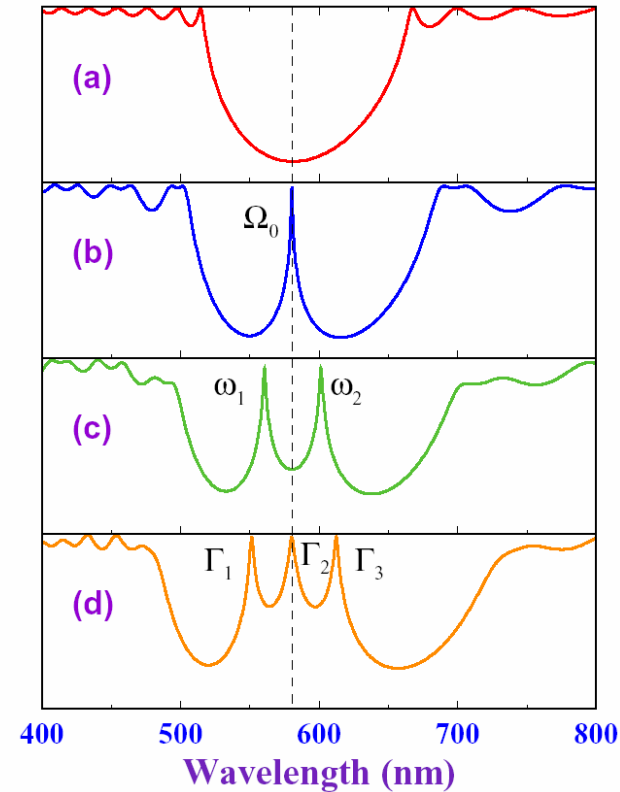


	n	d [nm]
Si_3N_4	2.10	70
SiO_2	1.47	97

Transmission (arb. units)



Transmission (arb. units)

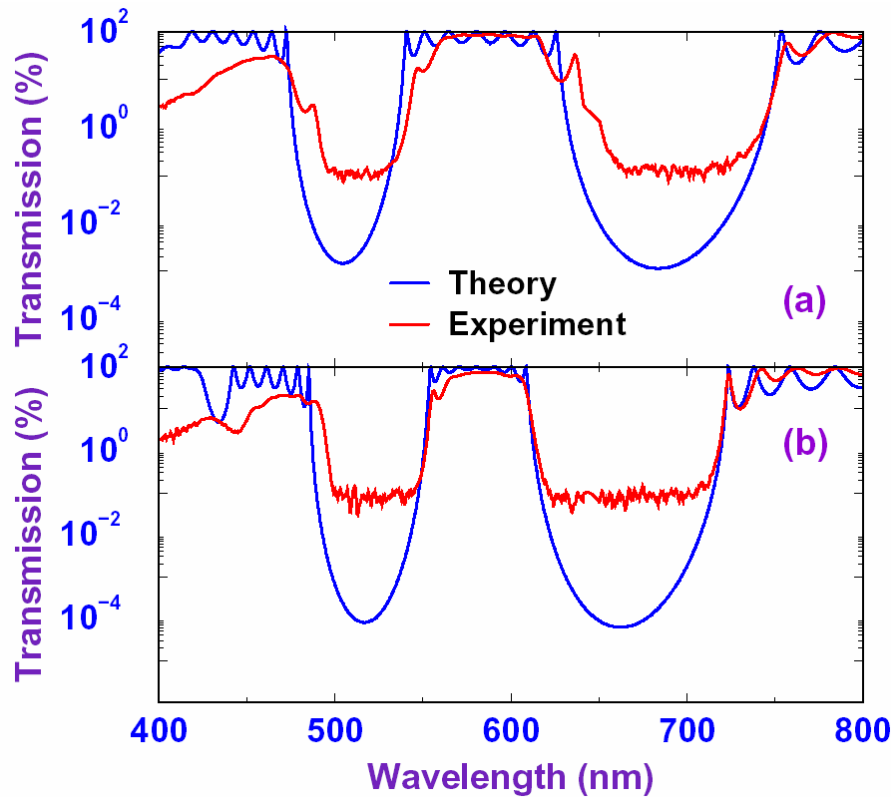
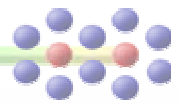


	Measurement [THz]	TMM [THz]	TB [THz]
Γ_1	490.08	491.30	489.85
Γ_2	516.53	516.80	516.83
Γ_3	543.65	542.81	544.10

Bayindir, *et al.*, Appl. Phys. A 72, 117 (2001); Appl. Phys. A 73, 125 (2001)

Experimental results agree well with TMM and TB predictions for the three coupled-cavities

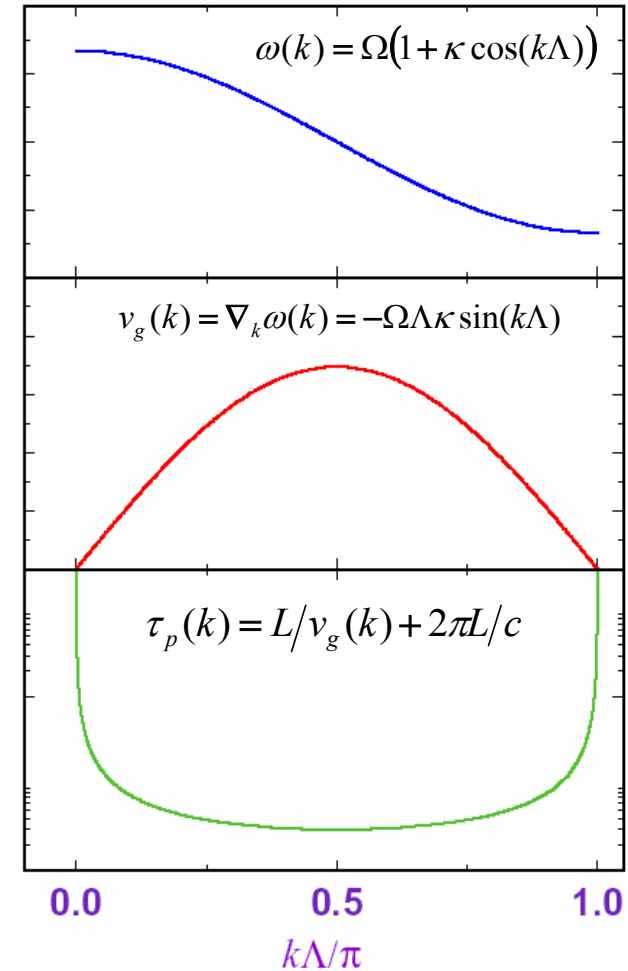
COUPLED-CAVITIES IN 1D STRUCTURES



$$\omega_k / \Omega$$

$$v_g / c$$

$$\tau_p \text{ (ps)}$$



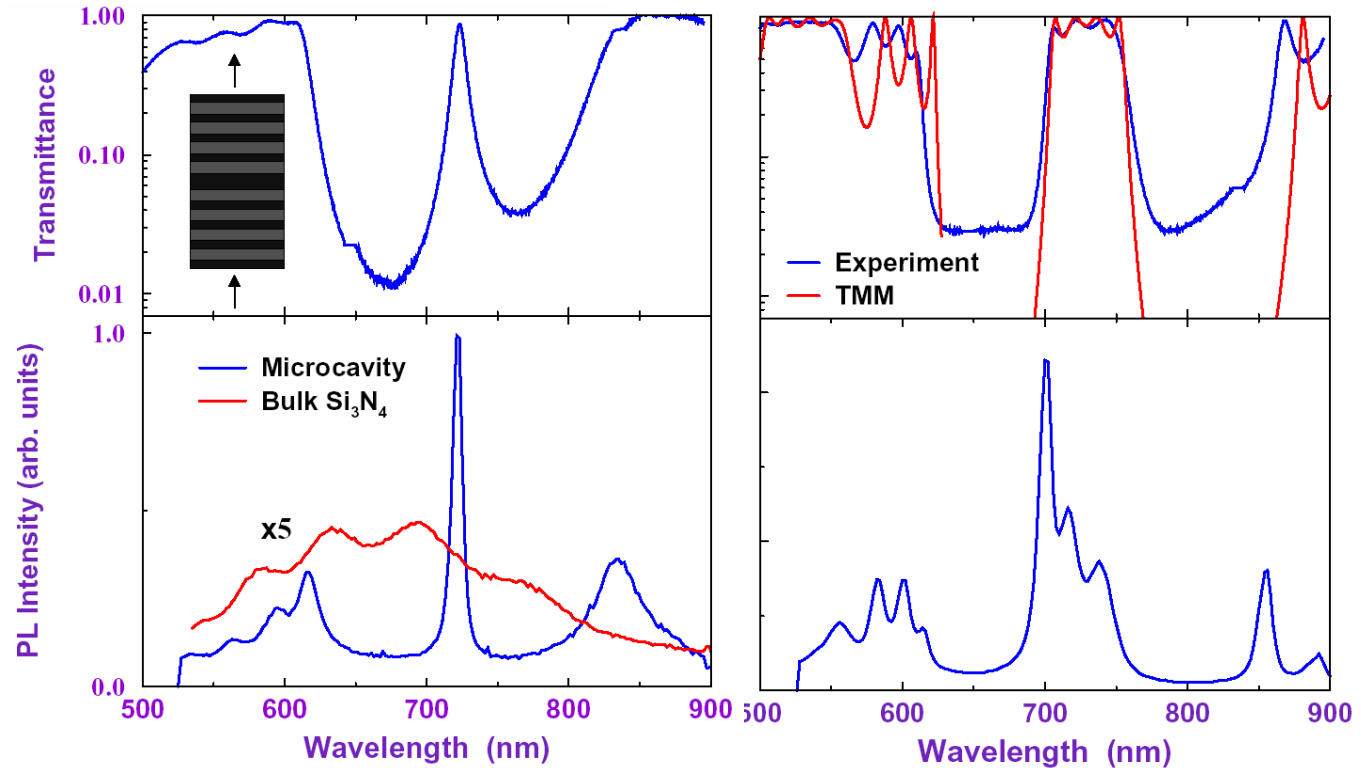
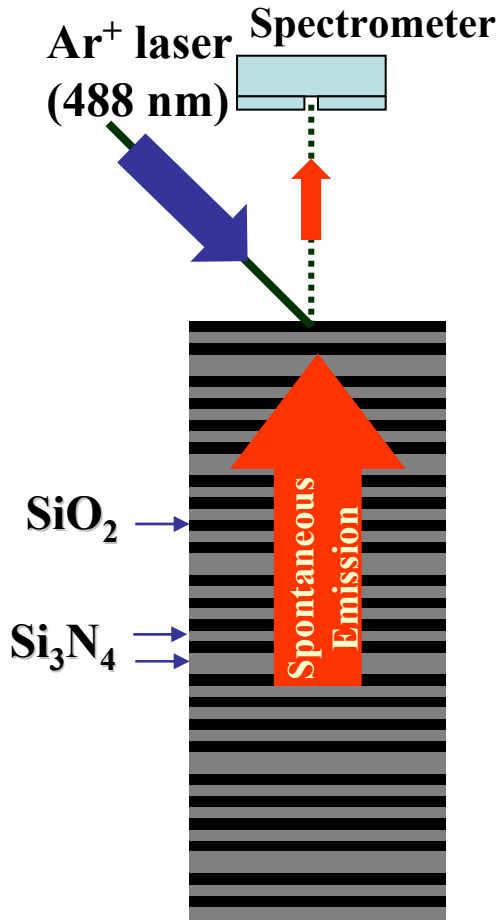
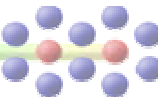
- ◆ Efficiency of the second harmonic generation process can be increased as a result of large optical field amplitude and low group velocity at the waveguiding band edges
- ◆ Nearly full transmission was measured throughout the CMC band
- ◆ The transfer matrix method results agree well with the experimental observations
- ◆ The position and bandwidth of waveguiding band can be adjusted by changing the thicknesses of the layers and the distance between the cavity layers

at the CMC
band edges

$$\begin{aligned} v_g &\rightarrow 0 \\ \tau_p &\rightarrow \infty \end{aligned}$$

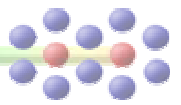
heavy
photon

PHOTOLUMINESCENCE FROM THE COUPLED-MICROCAVITY STRUCTURE

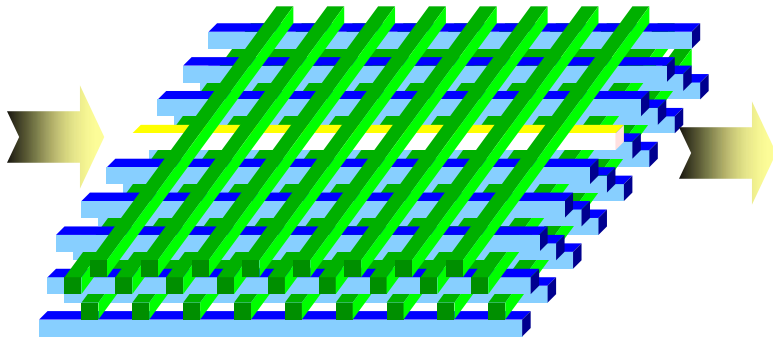


- ◆ The photoluminescence spectrum was strongly modified in the presence of Fabry-Perot microcavity
- ◆ A strong spontaneous emission was achieved for a wide range of wavelengths
- ◆ The spontaneous emission was significantly enhanced at the coupled-cavity band edges

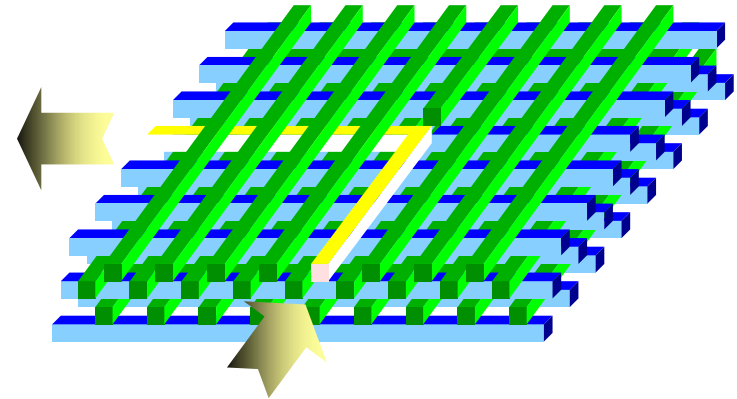
HIGHLY CONFINED WAVEGUIDES



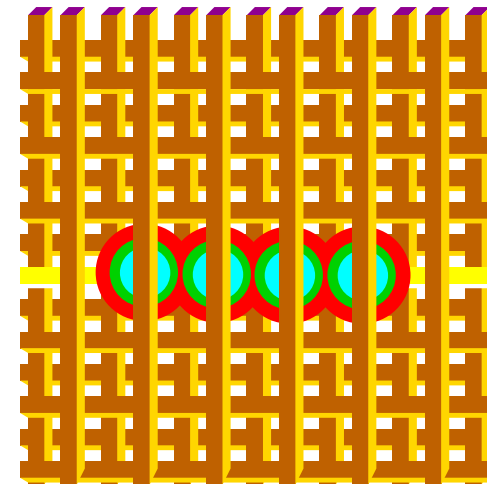
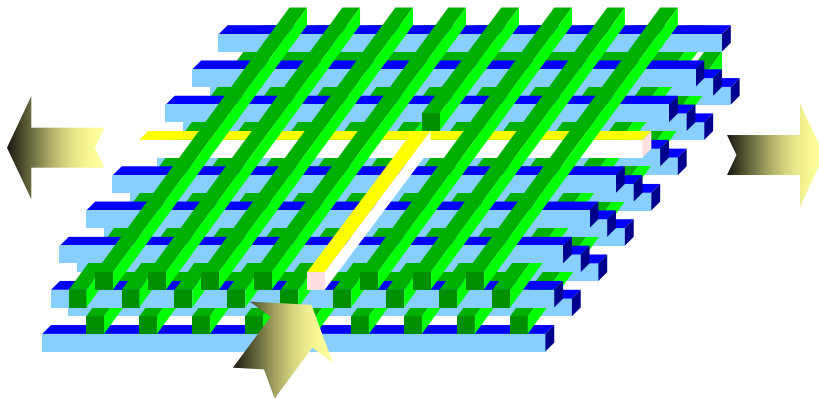
Straight Waveguide



Bended Waveguide



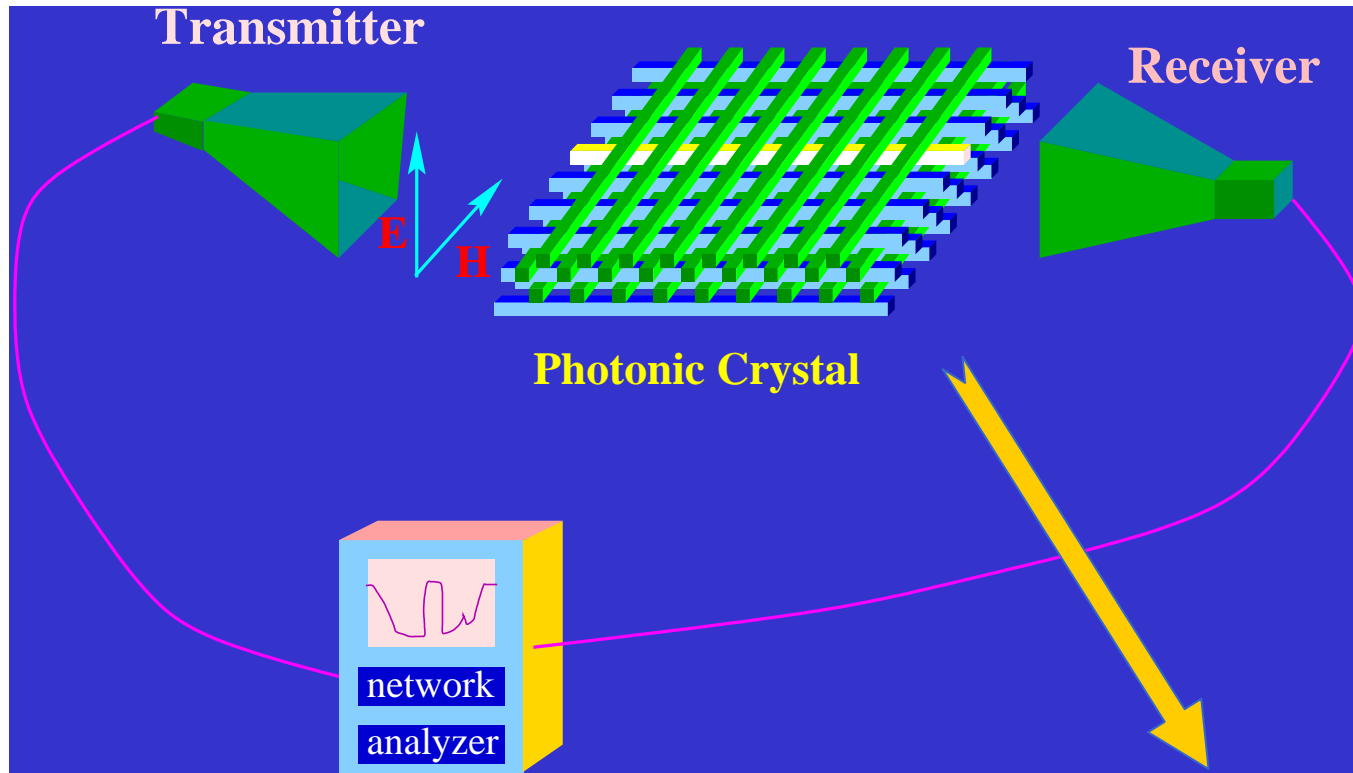
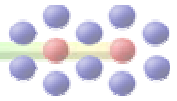
Power Splitter



Noda *et al*, APL 75, 3739 1999;
Bayindir *et al.*, PRB 63, 081107(R) (2001)

Full confinement of electromagnetic waves in 3D layer-by-layer photonic crystals

EXPERIMENTAL SETUP



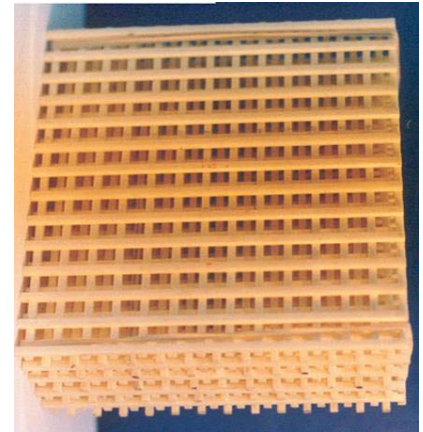
Symmetry: Face centered tetragonal (fct)

Material: Alumina of refractive index

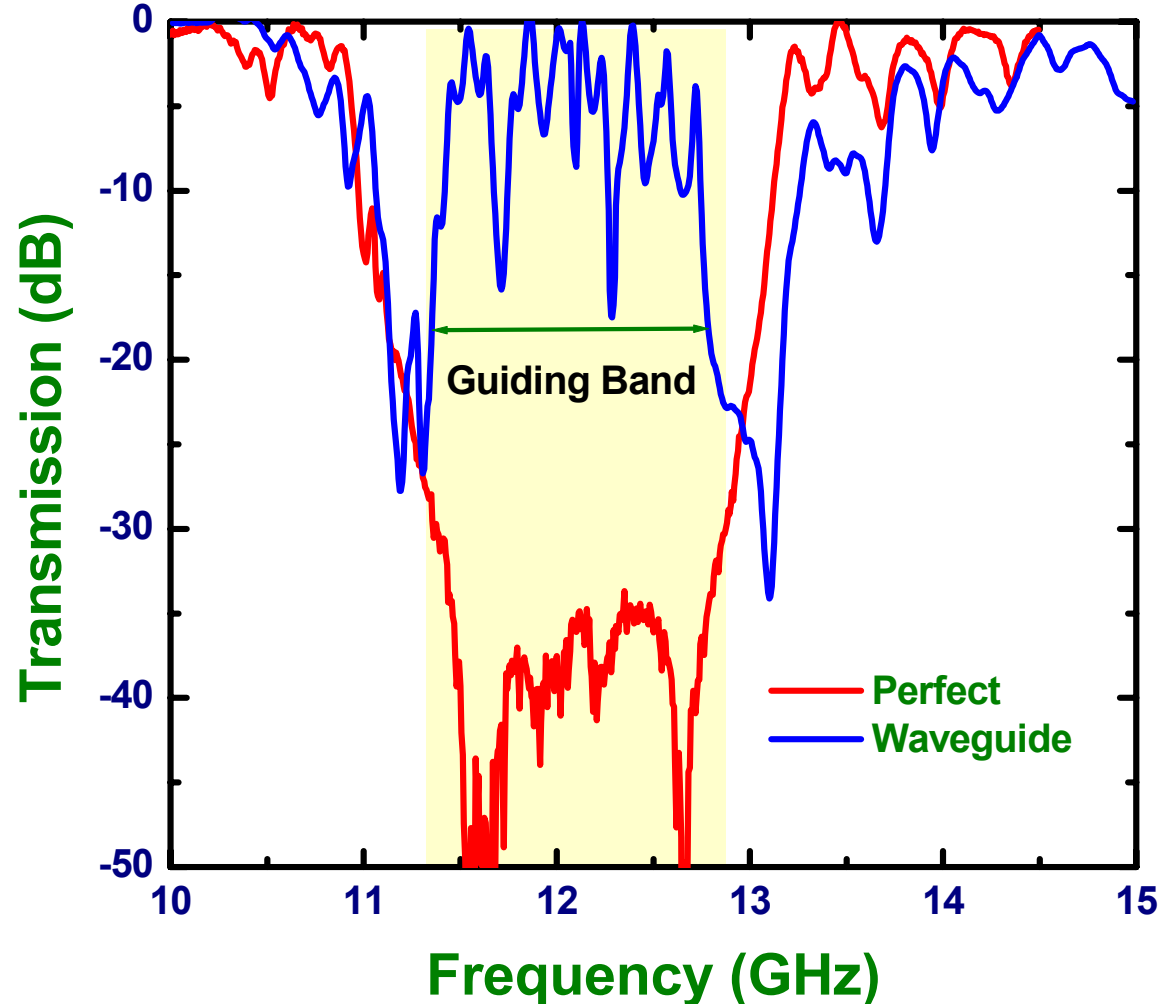
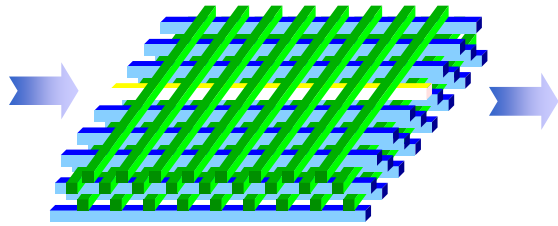
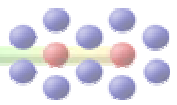
$\epsilon = 3.1$ at microwave frequencies

Dimensions: 0.32 cm \times 0.32 cm \times 15.25 cm

Photonic band gap: 10.6 GHz -12.8 GHz

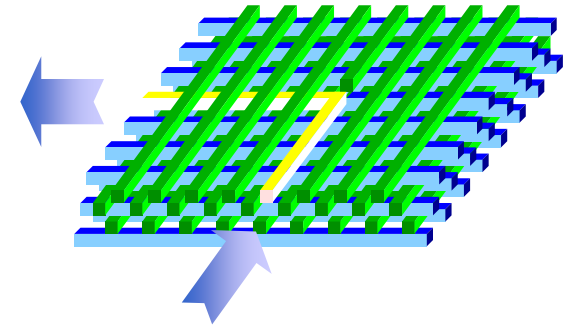
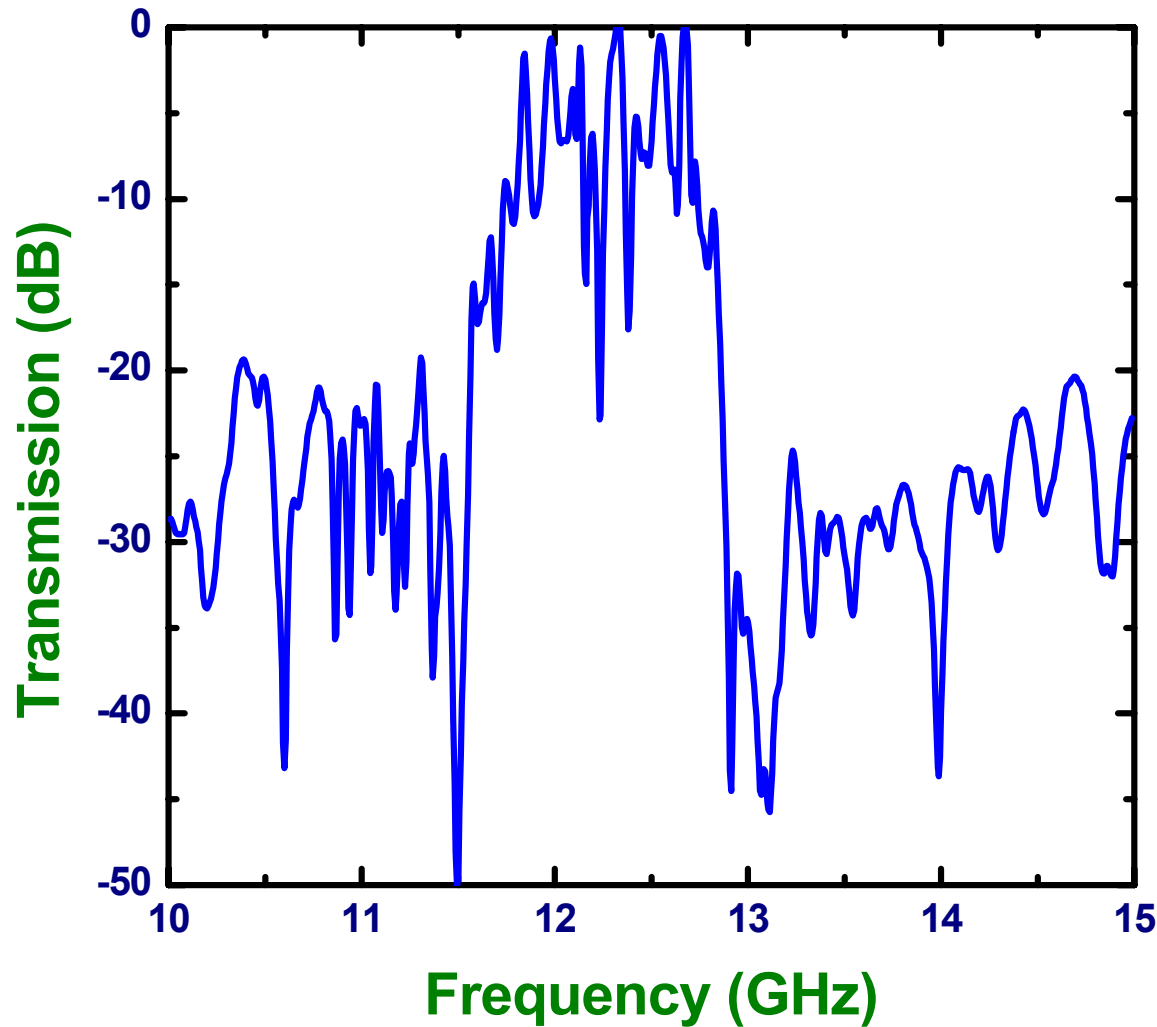
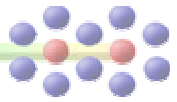


STRAIGHT WAVEGUIDE



- ▶ Nearly full transmission was achieved for certain frequencies
- ▶ The full transmission within the waveguiding band was a proof of how well the wave was confined and guided without loss

WAVEGUIDE BENT

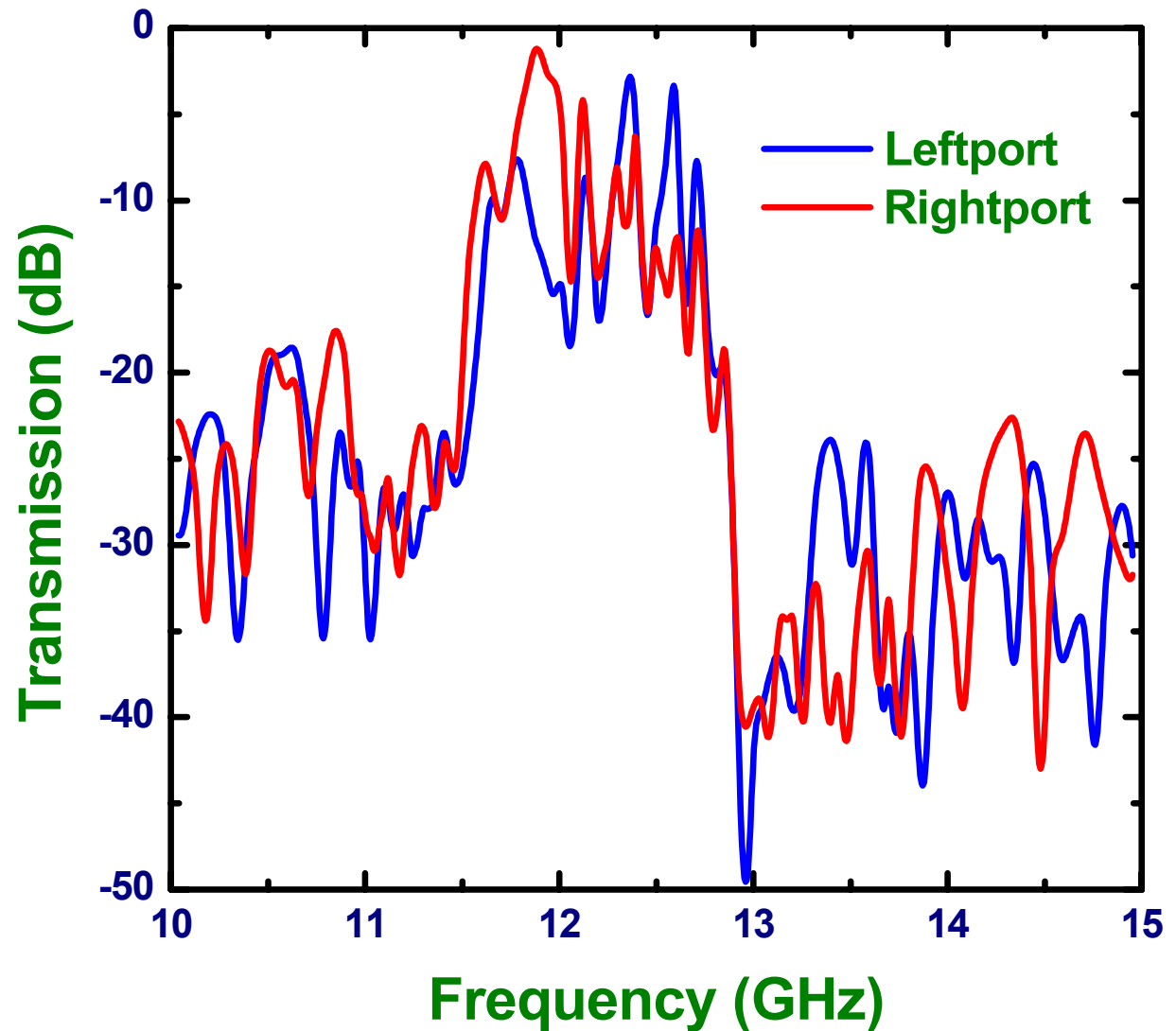
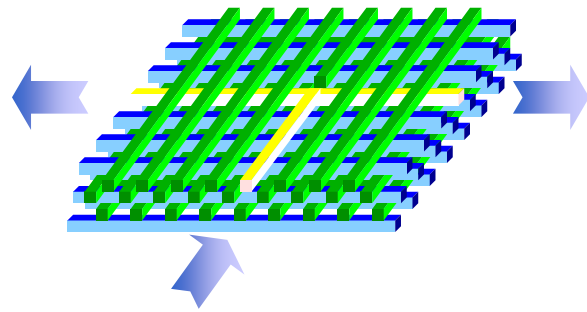
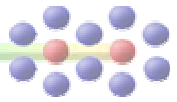


**Comparison with simulation
[Noda's Group, APL (1999)]:**

**The bending band covers 68%
of the stop band which is very
close to the simulation results
value of 67%.**

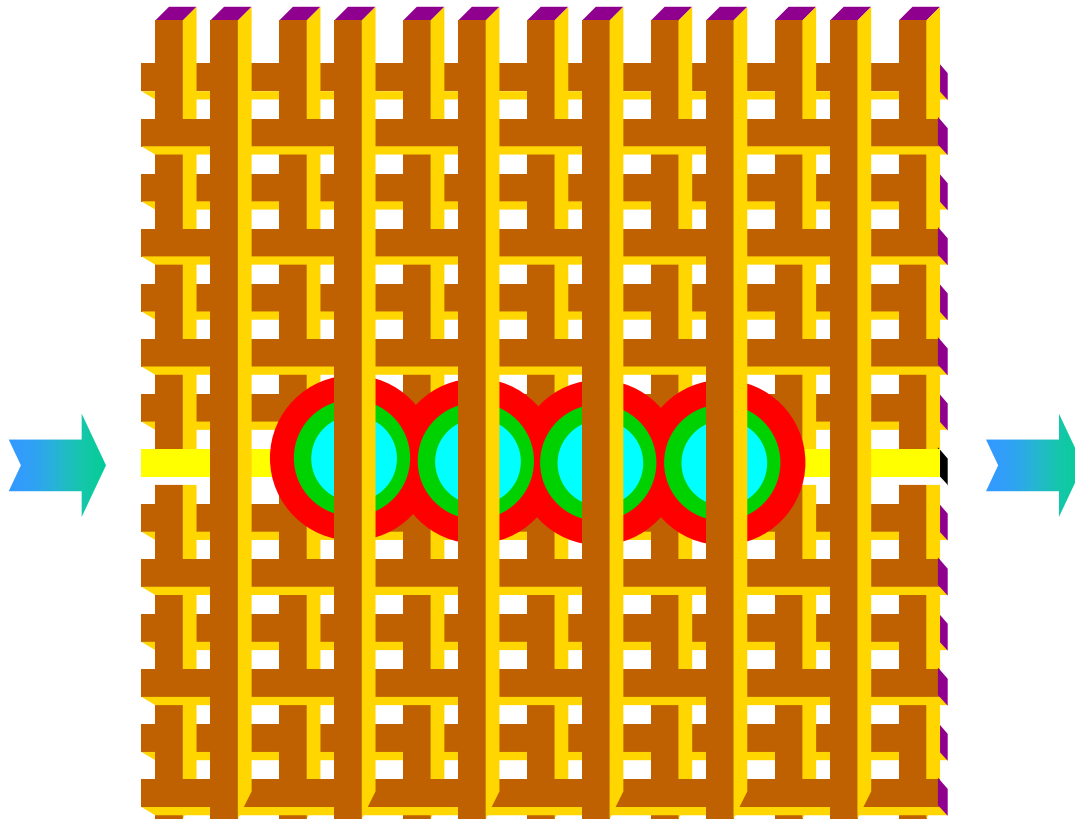
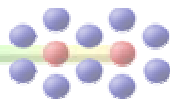
► The full transmission through a 90° bent was achieved for certain frequencies throughout the waveguiding band

POWER SPLITTER



- The electromagnetic power in the input port splits into the two output ports throughout the guiding band

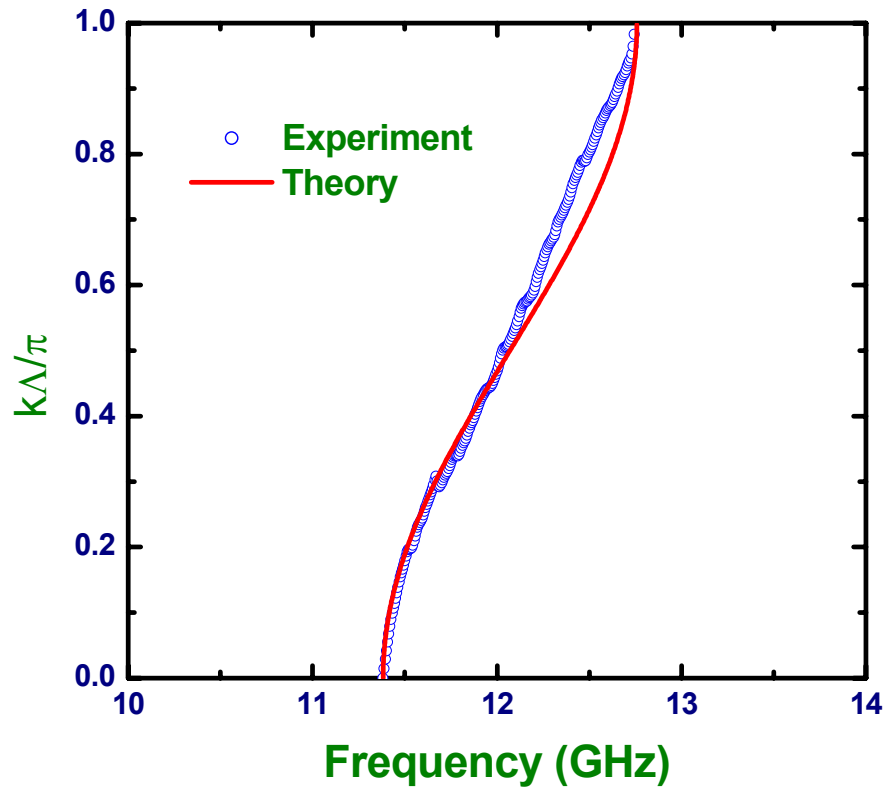
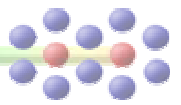
THEORETICAL MODEL: TIGHT BINDING APPROXIMATION



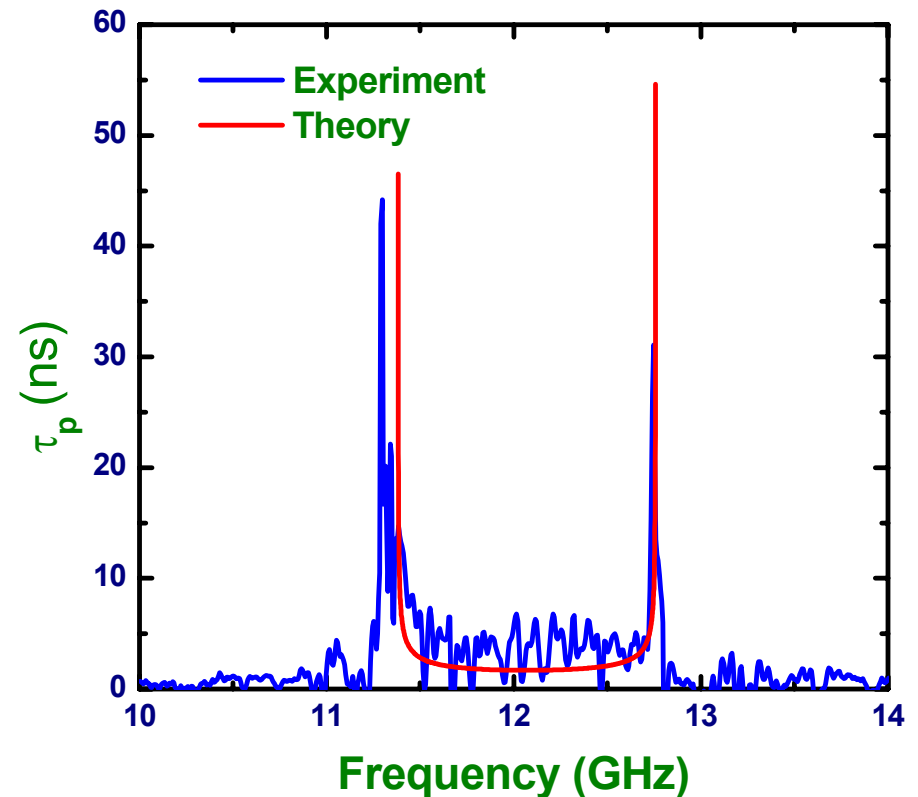
Each vacancy just below the removed rod behaves as a boxlike cavity

- The coupling between these localized cavity modes allows propagation of photons by hopping through the vacancy of the missing rod

DISPERSION RELATION & PHOTON LIFETIME



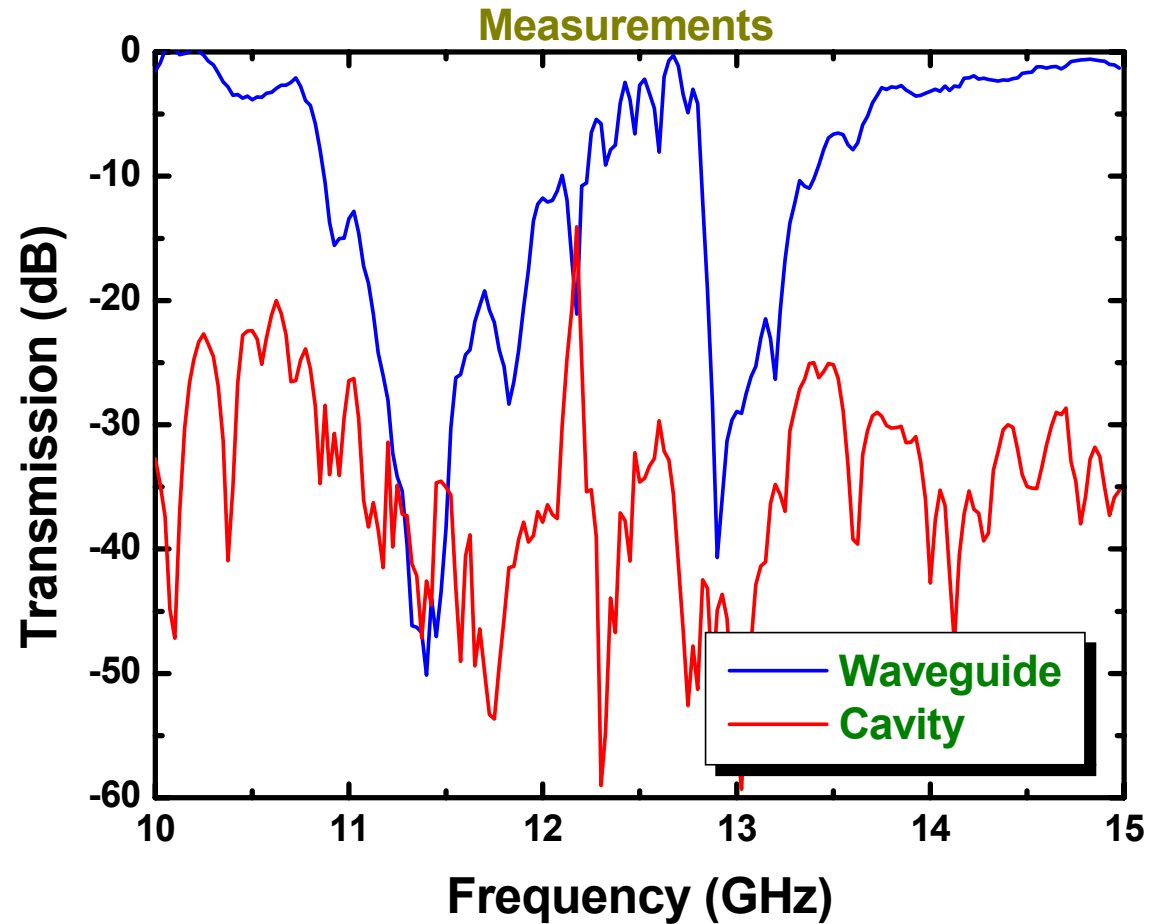
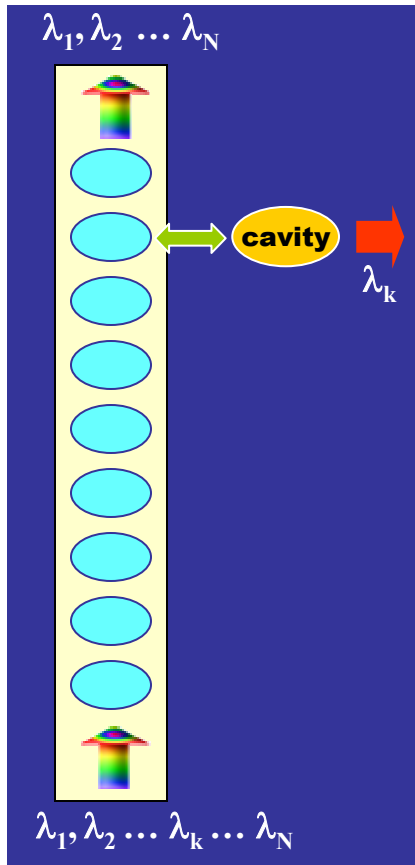
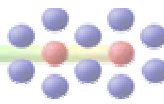
$$\omega(k) = \Omega(1 + \kappa \cos(k\Lambda))$$



$$\tau_p(k) = L/v_g(k) + 2\pi L/c$$

► Experimental results were in good agreement with the tight-binding approximation predictions

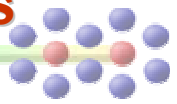
WDM APPLICATIONS: DROPPING A SELECTIVE WAVELENGTH



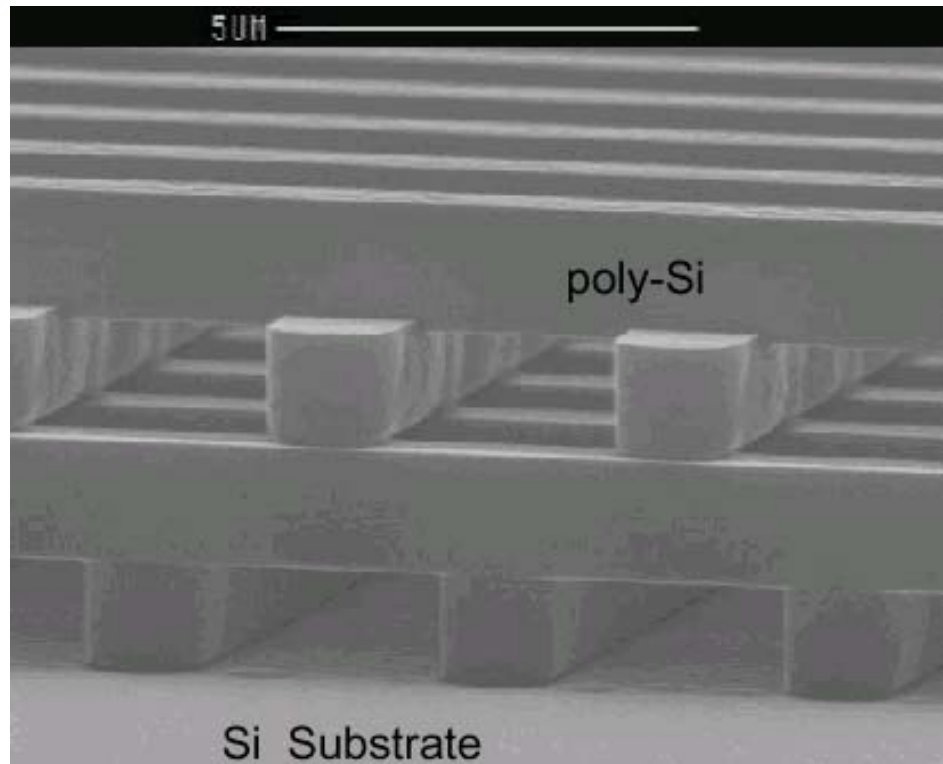
Bayindir and Ozbay [in preparation]

- ◆ Electromagnetic wave with a specific frequency can be dropped from the guided mode inside the waveguide.
- ◆ Tunability can be achieved by changing properties of the cavity.

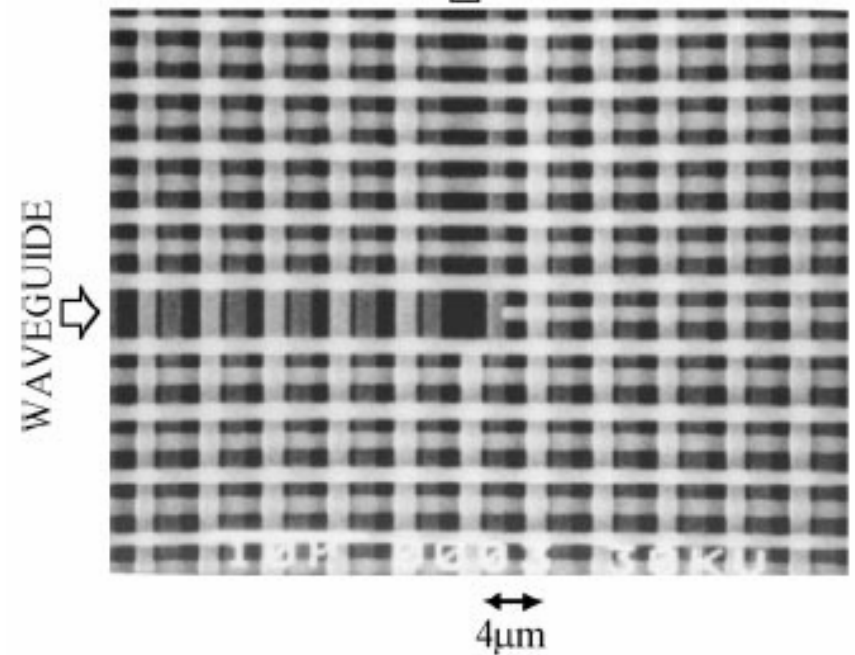
3D LAYER-BY-LAYER STRUCTURES AT OPTICAL WAVELENGTHS



Lin *et al*, Nature **394**, 251 (1998)

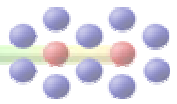


Noda *et al*, Science **289**, 604 (2000)



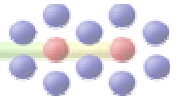
- ♦ Highly confined waveguides, waveguide bends, power splitter, add-drop filters, switches can be used in future ultrasmall optoelectronic integrated circuits.

SUMMARY



- ❖ Various applications of 1D, 2D, and 3D coupled-cavity structures were demonstrated
- ❖ The tight-binding approximation was successfully applied to the photonic structures
- ❖ The finite-difference-time-domain (FDTD) and the transfer matrix method (TMM) results agree well with our measurements

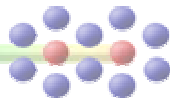
ACKNOWLEDGEMENTS



These works were supported by

- Turkish Department of Defense Grant No. KOBRA-01, Thales JP8.04
- NATO Grant No. SfP971970
- National Science Foundation Grant No. INT-9820646

MORE INFORMATION



<http://www.fen.bilkent.edu.tr/~bayindir>

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